

Analog and digital communication.

Communication Engg - I

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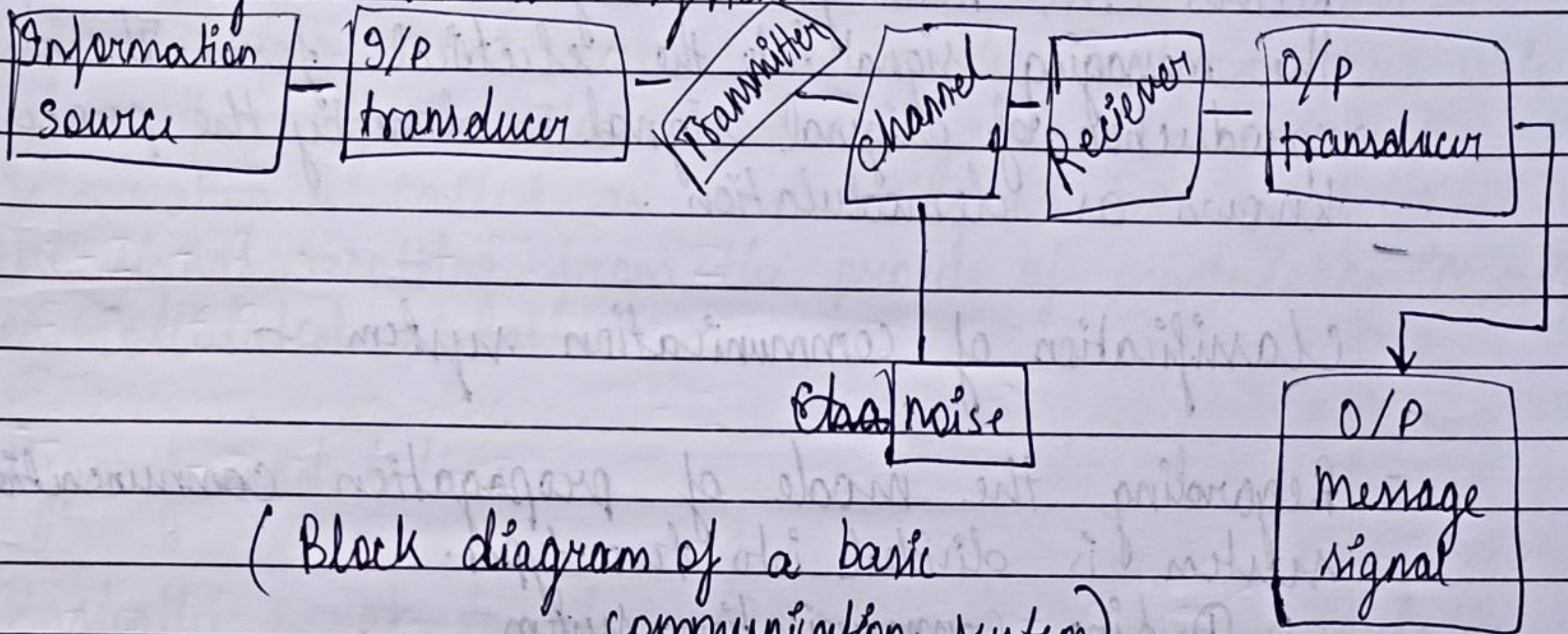
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Communication -

Communication is the process by means of which message or information transfer from source to destination.

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Elements of communication system -



Information source -

or A communication system basically communicates message of information. This message or information originates in the information source.

The function of information source is produce required message.

Input transducer - A transducer is a device which converts one form of energy into another form. Hence the input transducer is used to convert the non-electrical message or information into electrical signal.

Transmitter - The transmitter modifies the message signal for efficient transmission. The transmitter process the electrical signal from different aspects. In the transmitter the process of modulation is done such that this will produce suitable form of the signal which can be transmitted over the channel.

- Noise - Noise is an unwanted signal which tends to interfere with the original signal. Noise signal always has a random nature.

Receiver - The main function of the receiver is to reproduce the messaging signal into the electrical form. The reproduction of the original signal is done by the process known as demodulation.

Classification of communication system -

- Regarding the mode of propagation, communication systems are divided into two types.

① Line communication system

② Wireless or radio communication system.

Line communication system - In line communication system, the medium of transmission is the transmission line. This is also called the line channel. This means in line communication, the transmitter and receiver are connected to a wire through a wire or line.

Wireless or radio communication system - In wireless or radio communication, a message is transmitted through a space by electromagnetic waves called as radio waves. Radio waves are transmitted from the transmitter through a device called an antenna. Again, a receiving antenna intercepts the radio wave at the receiver. All the TV, radio, satellite communication are wireless or radio communication.

Amplitude modulation system -

Modulation - Modulation is defined as the process by means of which the ~~car~~ characteristics of signal called ~~carrier~~ carrier signal is ~~vary~~ varied in accordance with ~~acceder~~ accordance with the instantaneous value of another signal called modulating signal. Contain the information is called as modulating or baseband signal. The signal resulting from the process of modulation is called as modulated signal.

Types of modulation -

Basically is of two types ① Continuous wave modulation.
② Pulse modulation.

Continuous wave modulation - When the carrier wave is continuous in nature then the modulation process is called continuous wave modulation. Ex - Amplitude modulation and Angular modulation.

Pulse modulation - When the carrier wave is a pulse type waveform then the process of modulation is called pulse modulation. Ex - PAM (Pulse amplitude modulation), PWM (Pulse width modulation), PCM (Pulse code modulation).

Need for modulation -

- i) To reduce height of antenna.
- ii) When the free space is used as the transmitting medium or channel then message signal are transmitted and received by help of antenna.

iii) For efficient radio radiation and reception of the signal the antenna must have the length comparable to quarter wave length of the frequency used. Let the 5 kHz signal is transmitted without the process of modulation then the height of the antenna required for effective radiation is

$$L = \frac{\lambda}{4} = \frac{c}{f \cdot 4}$$

$$= \frac{3 \times 10^8 \text{ m/s}}{4 \times 5 \times 10^3 \text{ Hz}}$$

$$= 5 \text{ km}$$

where c = speed of light ($\approx 3 \times 10^8 \text{ m/s}$)

f = frequency of modulating signal

Then antenna height is totally impractically impractical to construct and install. If a ^{high} frequency carrier is used for modulation. If then the modulating signal is 3 MHz. Then the antenna height will become

$$L = \frac{\lambda}{4} = \frac{c}{f \cdot 4}$$

10^{8-6}

10^0

10^2

$$= \frac{3 \times 10^8 \text{ m/s}}{4 \times 3 \times 10^6 \text{ Hz}}$$

$$= 25 \text{ m}$$

$$\approx 25 \text{ m} = \frac{10^2 \cdot 10^2}{4}$$

$$= \frac{100}{4} = 25 \text{ m}$$

Then antenna height may be achieve practically. ~~It's~~

To reduce the noise - Noise can't completely eliminated from the communication system but with the help of several modulation scheme the effect of ^{the} noise, minimize. To remove interference. Another reason

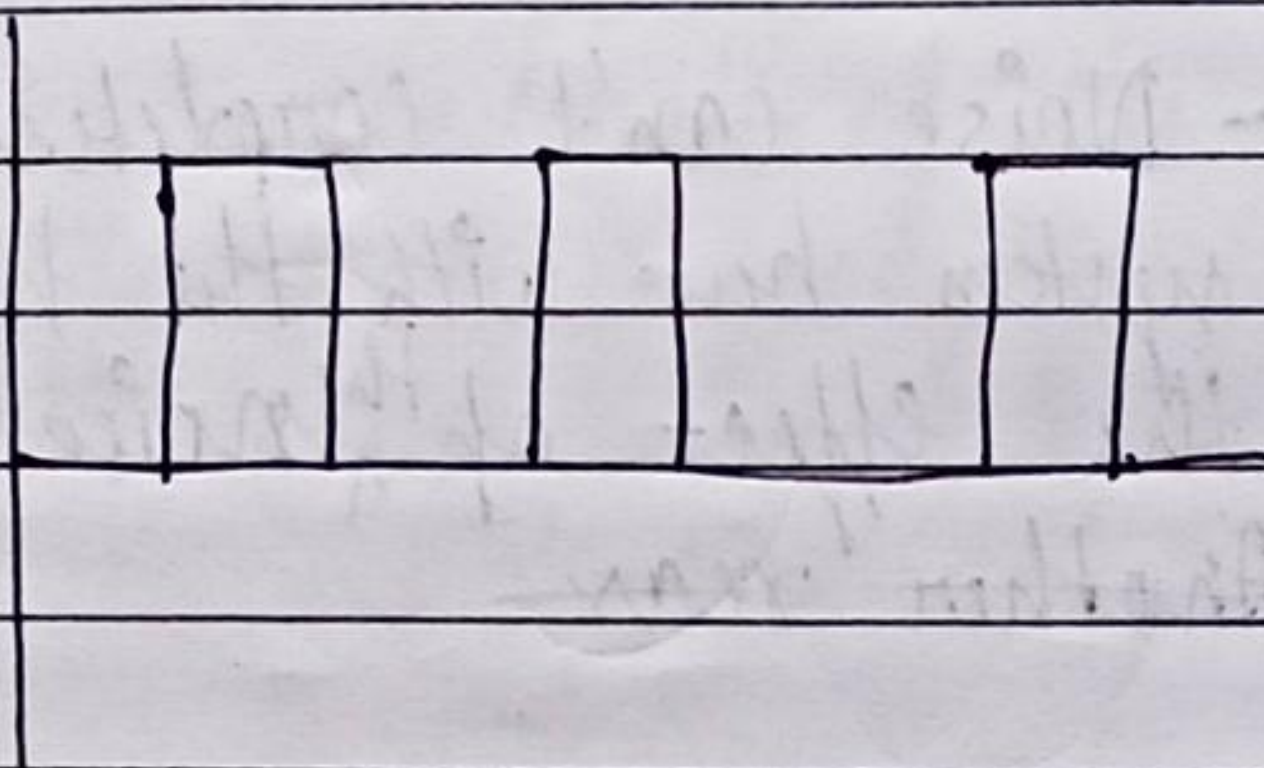
Another reason ^{for} not radiating ~~modul~~ modulating signal itself is the frequency wave ~~the~~ of the audio signal is 20Hz to 20KHz. In radio broadcasting there are several radio station. If modulation is not be use then all the station transmits the signal in the range of 20Hz to 20KHz. Due to transmission of the same range. The programme of the different station will get mixed of resulting interference. ~~Multiplex~~

Multiplexion - When a single channel is used between the transmitter and receiver for sending more than one signal at the same time then there is called multiplexing. There ~~in~~ multiplexing can be done using the process of multiplexion.

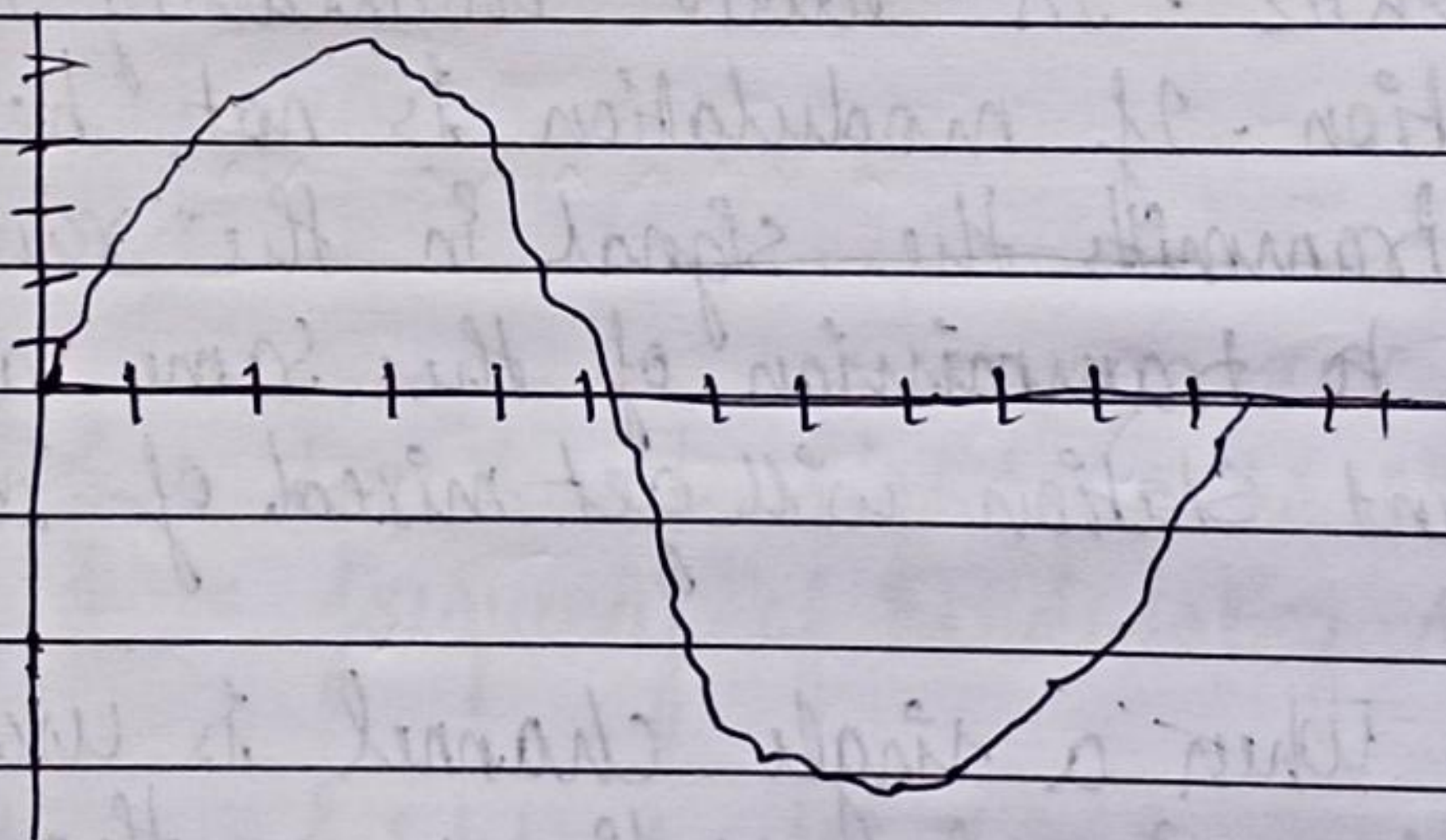
Analog signal - The analog signal is that type of signal which varies smoothly and continuously with time. This means that analog signal's are defined for every value of time and they take on continuous values of given time interval.

Digital signal - An alternating form of signal representation is that of a sequence of numbers, each number representing the signal magnitude at an instant of time. The resulting signal is called a digital signal. A digital signal is represented by only by digits therefore we can use binary number system to represent a digital signal. In a binary system each digit in the number

takes on only two possible values denoted 0 and 1.



digital signal



analog signal

The wave form is a pulse train with zero voltage representing zero signal and positive five voltage representing logic 1.

Conversion of analog to digital ~~an~~ signal -

Sampling Theorem -

The statement of sampling theorem can be giving as the following -

- 1) A band limited signal of finity energy which has no freq. components higher than f_m Hz is completely described by its sample values at uniform intervals less than or equal to $\frac{1}{2f_m}$ or $\frac{1}{2}$ times of f_m second a part
- 2) A band limited signal of finity energy which have no frequency components higher than f_m Hz may be completely recovered by from the knowledge of its samples taken at the ^{rate} of $2f_m$ samples per sec.
- 3) Combining these two parts the sampling theorem states that a continuous time signal may be completely represented in its sample and recover back if the sampling frequency $f_s \geq 2f_m$

where f_s is ~~the~~ the sampling frequency.

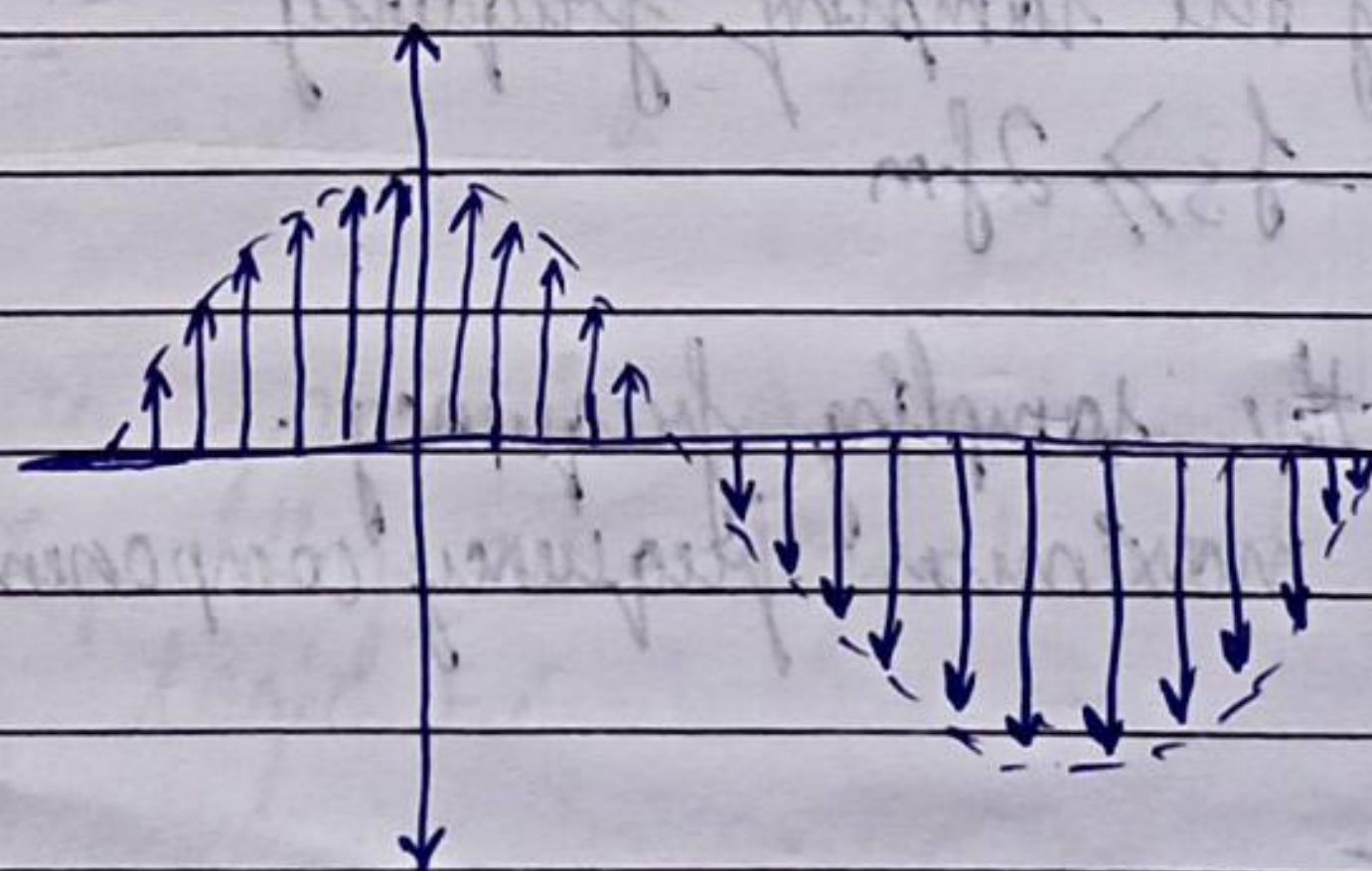
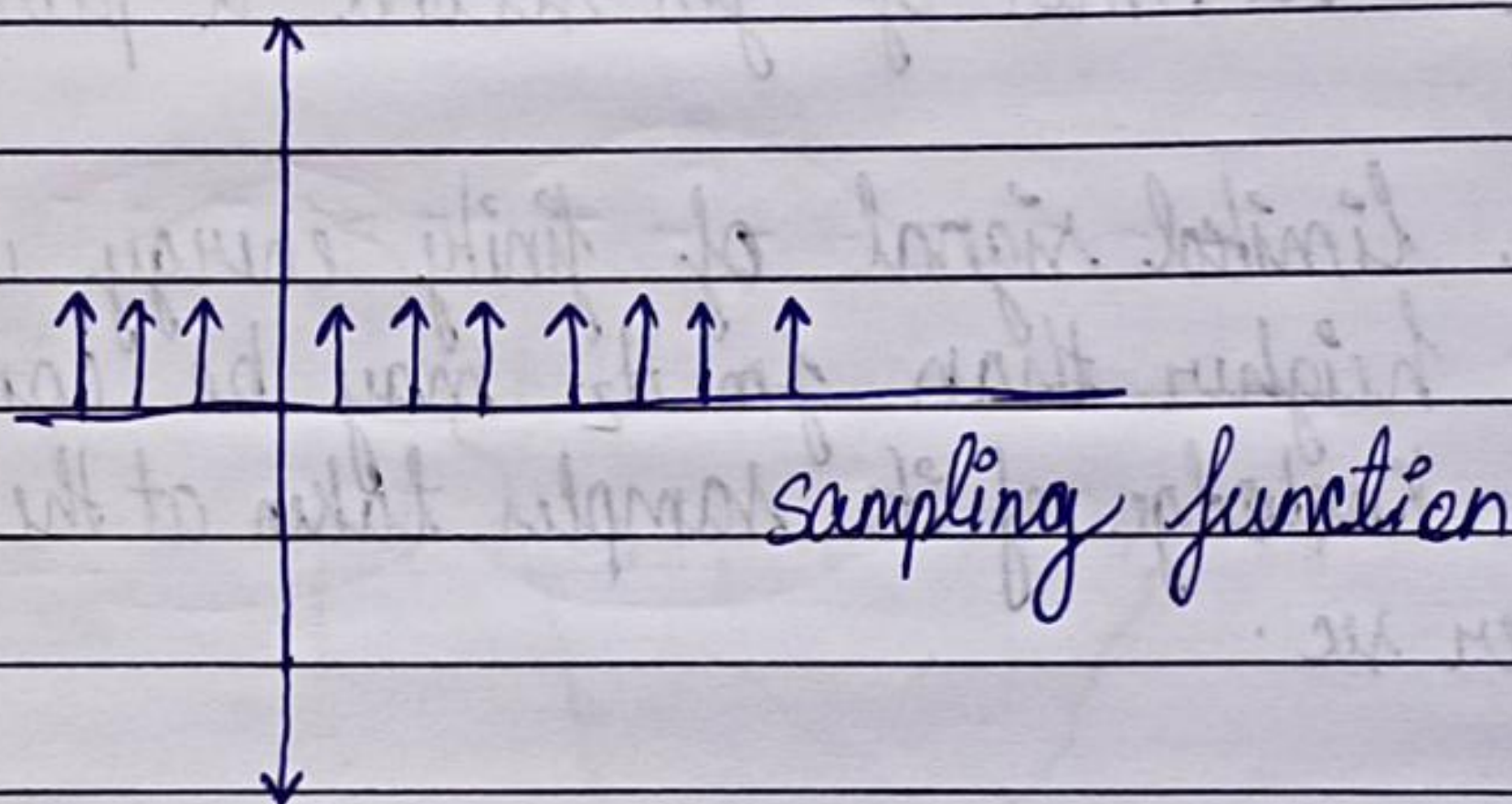
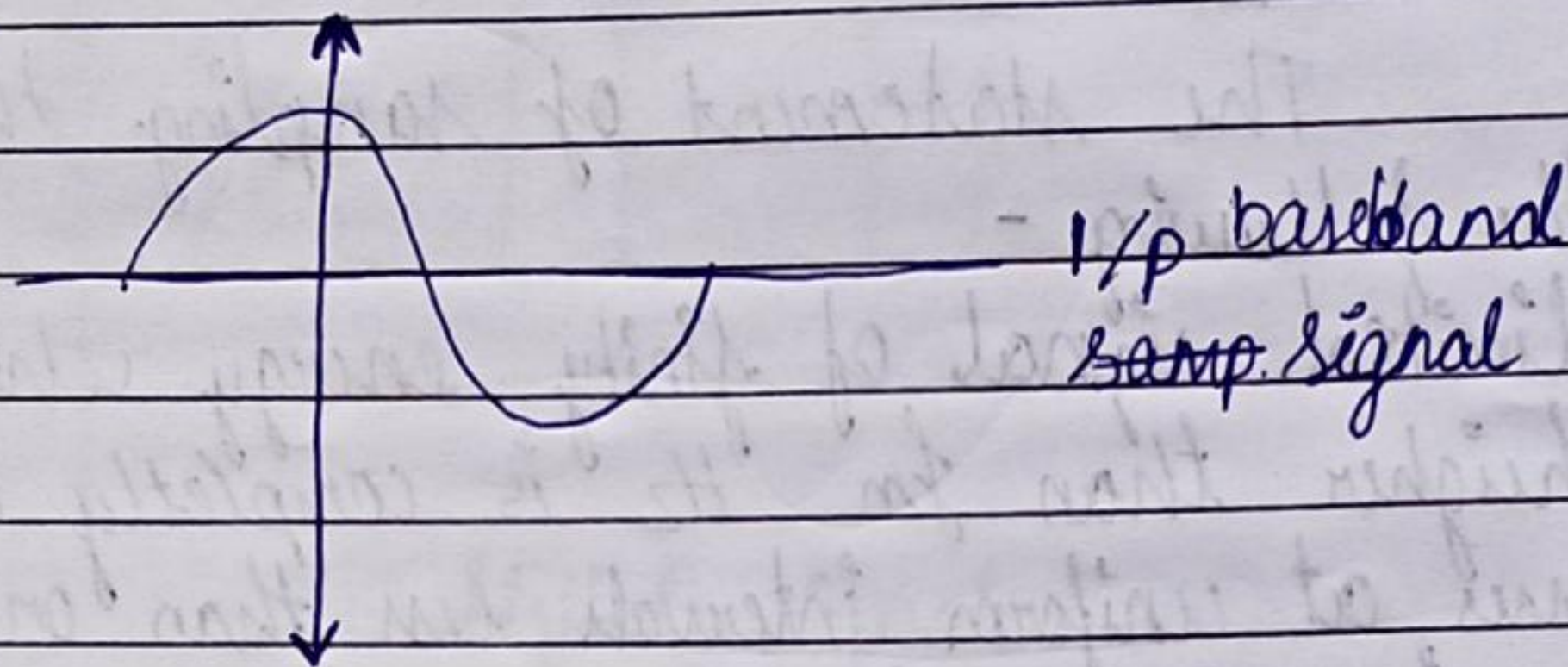
f_m is the maximum frequency component present in the signal.

* Types of sampling -

There are ~~two~~ ^{three} types of sampling techniques -

- ① Impulse / ideal / Instantaneous Sampling
- ② Natural Sampling
- ③ flat top / rectangular sampling

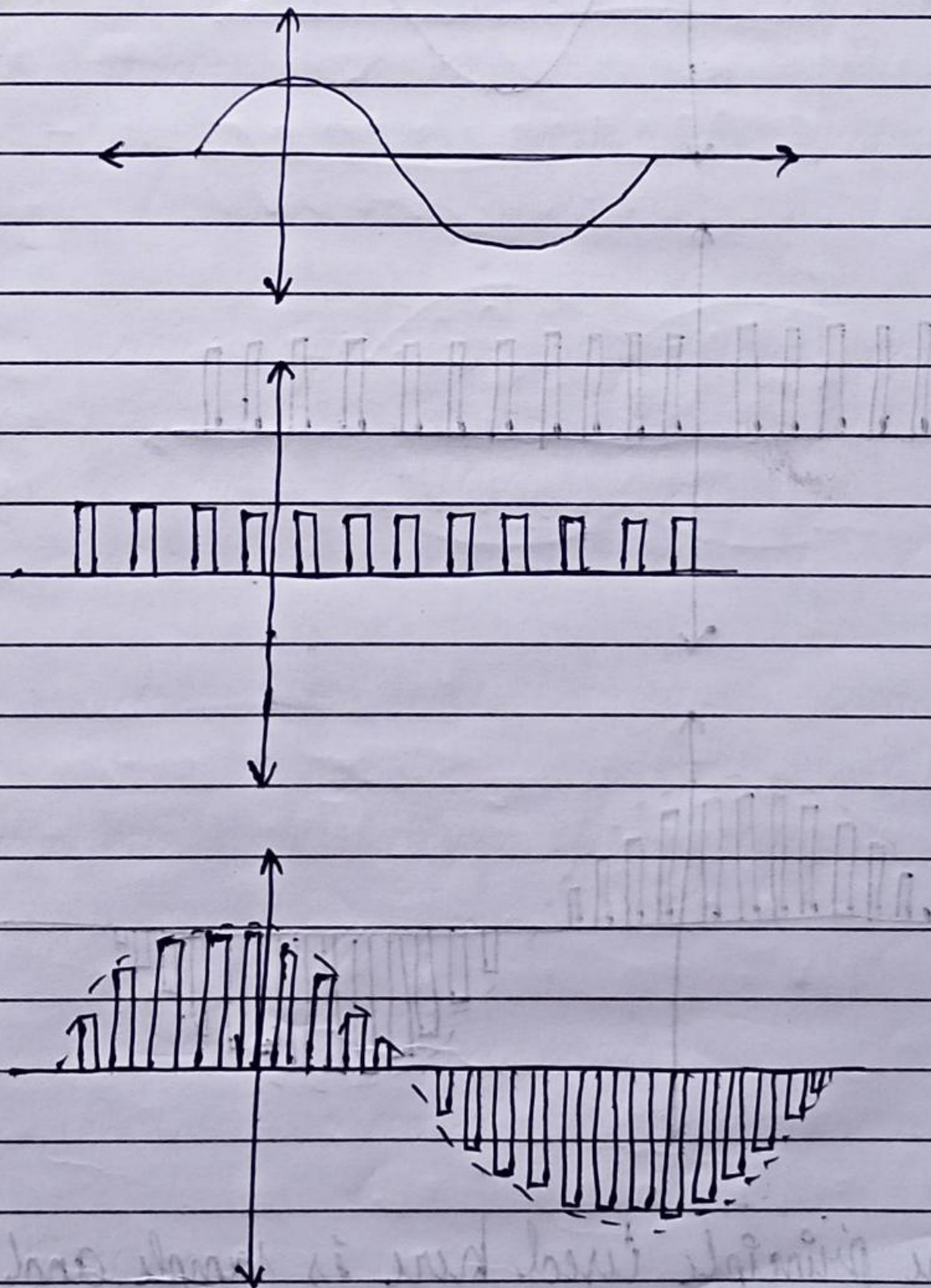
① Impulse / ideal / Instantaneous Sampling - Here the principle used as multiplication



- Noise Interference is maximum
- The sampling function is trend of impulse having width ($\tau \approx 0$)
- At any instant the amplitude of the sample signal ~~set~~ = Input signal.

- As the width of sample signal tends to zero the transmitted power is negligible.
- It is not practically used.

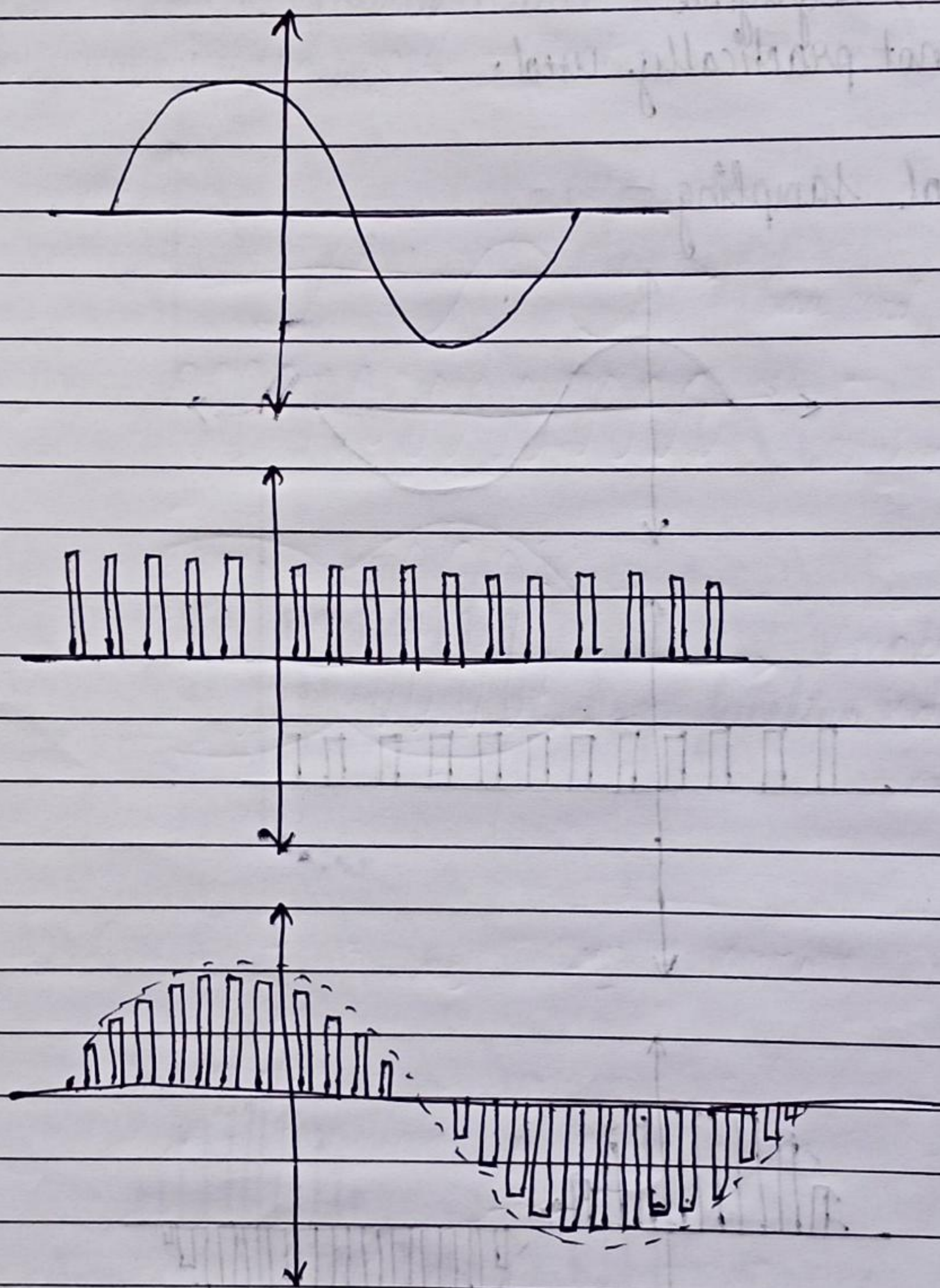
② Natural sampling -



Here the principle used is chopping.

- The noise interference is minimum.
- The sampling function is trend of pulse width having τ .
- At any instant the amplitude of the sample signal = input signal.
- It is practically used.

③ Flat top / rectangular sampling -



Here the principle used here is sample and hold.

- The noise interference is maximum
- The sampling function is a train of pulse
- At any instant the amplitude of sampling signal a = amplitude of the input signal at the instant of starting edge of the pulse.

Bandwidth limitation -

- The frequency range or the band of frequency needed for a particular given transmission is known as Bandwidth.
- The information theory states that the greater is the transmission bandwidth of a communication system the more is the information that can be transmitted. Therefore an AM radio receiver cannot reproduce all the information contain in the music because there will ~~be~~ required the bandwidth of 30kHz.

Q. what are the limitation of communication system?

Ans ① Noise limitation

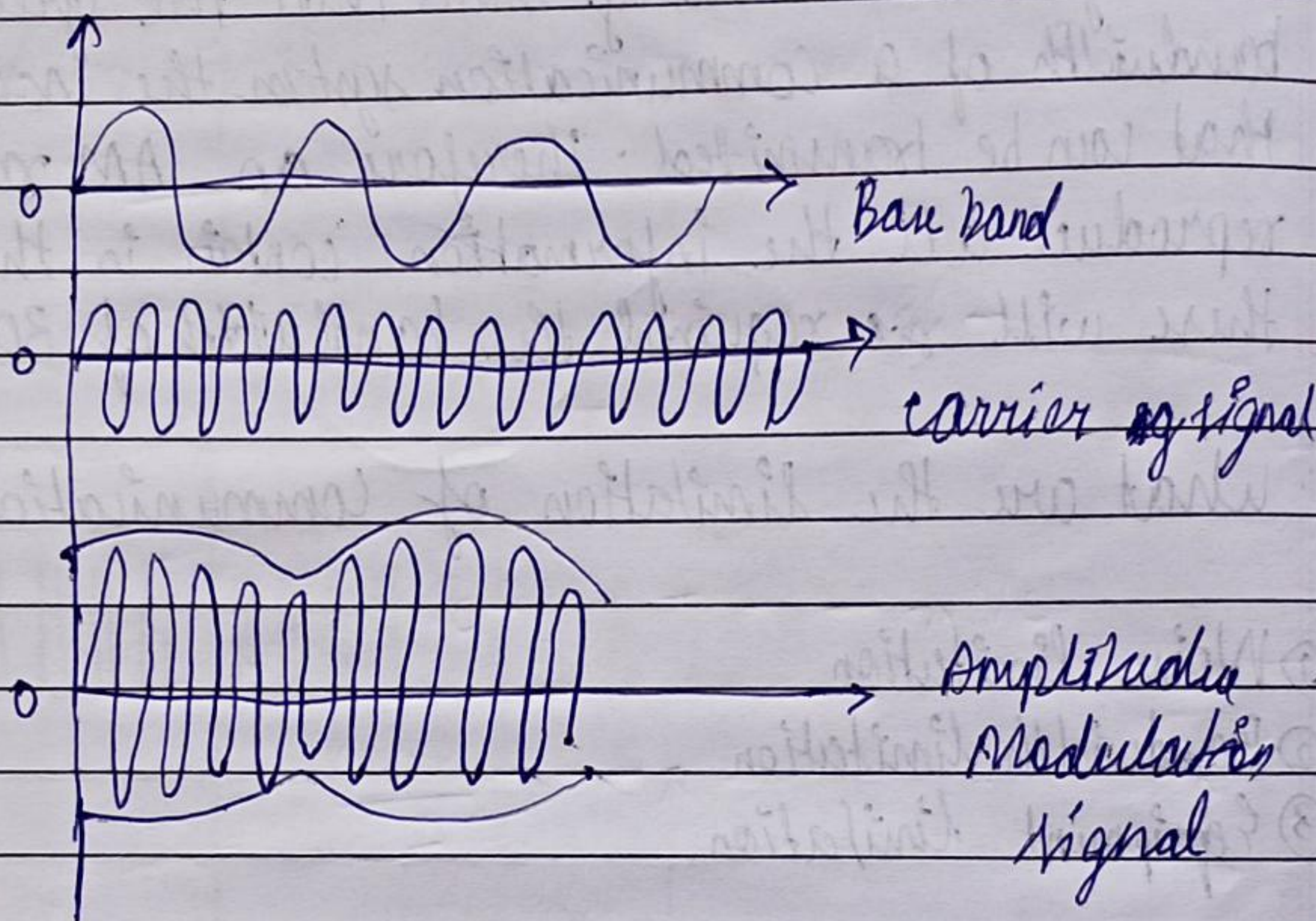
② Bandwidth limitation

③ Equipment limitation

Q. what is the role of bandwidth in the communication?

Ans Bandwidth is the total range of frequency

- Amplitude modulation - In Amplitude modulation amplitude of the carrier signal is changed with respect to base band signal keeping frequency and phase constant.



Let ~~the~~ $V_c(t) = V_{mc} \sin \omega_c t \rightarrow$ carrier signal.

V_m = amplitude of carrier signal
 ω_c = Angular of carrier signal

$$\text{Let } V_m(t) = V_m \sin \omega_m t$$

V_m = amplitude of the modulating signal
 ω_m = Angular of modulating signal.

$$V_c \propto V_m(t)$$

$$= k V_m(t) \quad \text{if } k = 1$$

$$M_a = \frac{V_m}{V_c} \quad \text{modulation index}$$

Derive the expression of amplitude modulation signal.

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$$V_c = V_m(t)$$

Here, amplitude of the modulated signal, -

$$V_c + V_m \sin \omega_m t$$

Now the expression the amplitude modulated signal

$$S_{a.m}(t) = (V_c + V_m \sin \omega_m t) \sin \omega_c t$$

$$= V_c \left(1 + \frac{V_m}{V_c} \sin \omega_m t \right) \sin \omega_c t$$

$$= V_c (1 + m_a \sin \omega_m t) \sin \omega_c t$$

$$= V_c (\sin \omega_c t + m_a \sin \omega_m t \sin \omega_c t)$$

$$= V_c \sin \omega_c t + M_a V_c \sin \omega_m t \times \sin \omega_c t$$

$$\begin{aligned} \cos C - \cos D &= -2 \sin \left(\frac{C+D}{2} \right) \sin \left(\frac{C-D}{2} \right) \\ &= 2 \sin \left(\frac{C+D}{2} \right) \sin \left(\frac{D-C}{2} \right) \end{aligned}$$

$$= V_c \sin \omega_c t + \frac{M_a V_c}{2} 2 \sin \omega_m t \cdot \sin \omega_c t$$

$$= V_c \sin \omega_c t + \frac{M_a V_c}{2} [\cos(\omega_c - \omega_m)t - \cos(\omega_c + \omega_m)t]$$

$$= V_c \sin \omega_c t + \frac{M_a V_c}{2} \cos(\omega_c - \omega_m)t + \frac{M_a V_c}{2} \cos(\omega_c + \omega_m)t$$

$$\cos(\omega_c + \omega_m)t$$

frequency - reciprocal of time period

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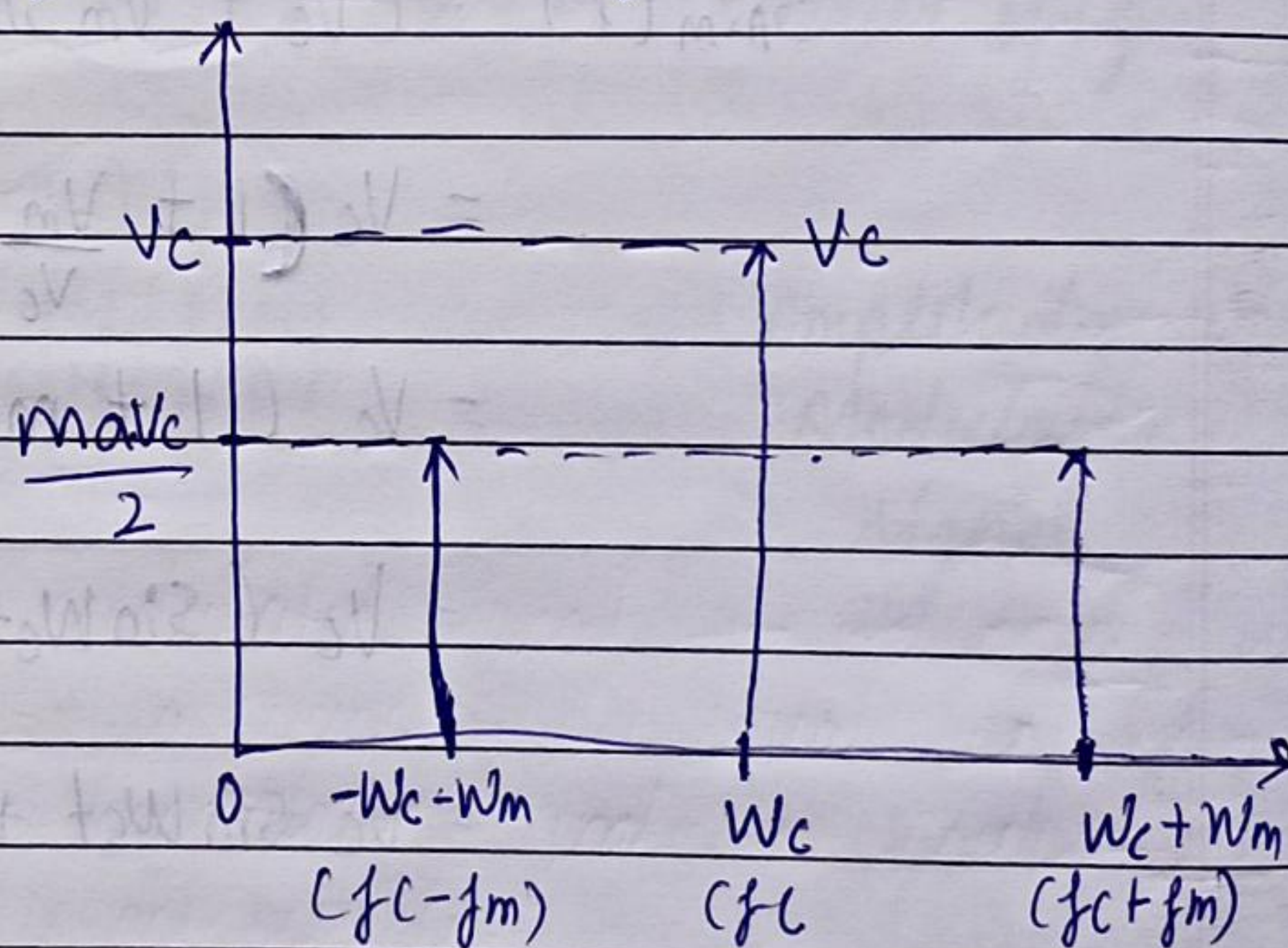
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The expression contains three terms first term is the unmodulated carrier having amplitude V_c .

Second term is the upper sign band having amplitude $\frac{M_a V_c}{2}$

Third term is the lower sign band (L.SB) having amplitude $-\frac{M_a V_c}{2}$.

Frequency spectrum of modulated signal -



Q Define communication channel?

Ans It is the connection between the transmitter and receiver are linked through the communication channel. Communication channel may be wireline or wireless or optical fiber?

Q Define channel bandwidth?

Ans It is the maximum possible range of frequency that can be used for the transmission.

$$B.W = f_2 - f_1 = \Delta f$$

Q Define transformation power ?

Ans There is the power that can be put in the signal being transmitted.

CALCULATION the bandwidth of ^{amplitude} modulated signal -

$$\begin{aligned} \text{for } B_{\text{BW}} = \Delta f &= f_c + f_m - (f_c - f_m) \\ &= f_c + f_m - f_c + f_m \\ &= f_m + f_m \\ &= 2 f_m \end{aligned}$$

$f_m \rightarrow$ original frequency.

• Modulation index - $M_a = \frac{V_m}{V_c}$

It is the ratio of maximum amplitude of modulating signal to the maximum amplitude of carrier signal.

There are three degree of modulation depending upon amplitude of carrier signal and modulating signal.

1) Under modulation ($M_a < 1$) - For under modulation index M_a is less than 1.

$$\begin{aligned} M_a &< 1 \\ \frac{V_m}{V_c} &< 1 \quad V_m < V_c \end{aligned}$$

Here the ^{envelope} ~~envelope~~ of the amplitude modulated signal will not reach to the zero axis amplitude axis. So, modulating signal can be properly recovered from the modulated signal.

using envelope detector.

2) Critical modulation ($M_a = 1$) — $V_m = V_c$

Here envelope of modulated signal just reaches the zero amplitude axis and the modulated signal can be recovered by using envelope detector.

3) Over modulation $M_a > 1$ —

$$\frac{V_m}{V_c} = 1$$

$$V_m > V_c$$

Here the envelope of modulated signal ~~ex~~ ~~pr~~ crosses the zero amplitude axis. So a portion of the signal can't be ~~proper~~ ~~preserved~~ in the modulated signal. So proper recovery of modulating signal is not possible.

Imp Power relation in amplitude modulated signal -

We know that amplitude modulated signal has three components. These are unmodulated carrier upper side band and lower side band. So the total power of AM wave is the sum of carrier power and the powers in the side bands.

$$P_T = P_c + P_{USB} + P_{LSB}$$

where,

P_T = Total power

P_c = Un modulated carrier power

P_{USB} = Power of upper side band

P_{LSB} = Power of lower side band

$$= \frac{(V_{carrier})^2}{R} + \frac{(V_{USB})^2}{R} + \frac{(V_{LSB})^2}{R}$$

where, all the three voltages are in RMS value and R is the characteristic impedance of antenna in which power is dissipated. So, the carrier power is $P_c = \frac{(V_{carrier})^2}{R}$

$$\begin{aligned} P_c &= \frac{(V_{carrier})^2}{R} \\ &= \frac{V_{carrier}^2}{R} \\ &= \frac{(V_c / \sqrt{2})^2}{R} \\ &= \frac{V_c^2}{2R} \end{aligned}$$

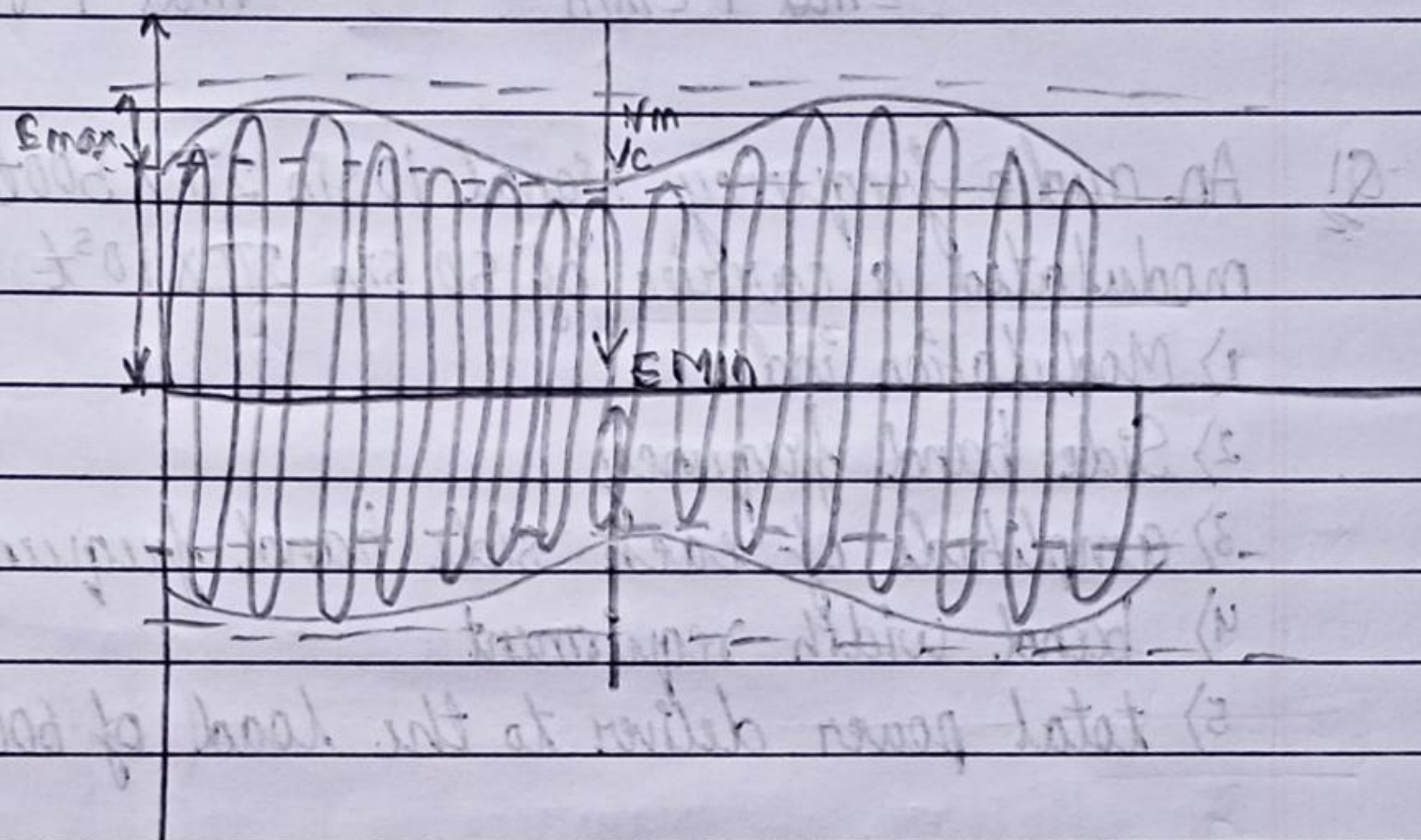
The side band power is

$$\begin{aligned} P_{USB} &= P_{LSB} = \frac{V_{USB}^2}{R} \\ &= \left(\frac{m V_c}{2\sqrt{2}} \right)^2 \times \frac{1}{R} = \frac{m^2 V_c^2}{8R} \end{aligned}$$

$$P_T = \frac{V_c^2}{2R} + \frac{m^2 V_c^2}{8R} + \frac{m^2 V_c^2}{8R}$$

$$\Rightarrow P_T = \frac{V_c^2}{2R} + \frac{m^2 V_c^2 + m^2 V_c^2}{8R} = \frac{V_c^2}{2R} + \frac{2m^2 V_c^2}{8R}$$

$$m = \frac{V_{\max} - V_{\min}}{V_{\max} + V_{\min}}$$



$$E_{\max} = E_{\min} + 2V_m$$

$$E_{\max} - E_{\min} = 2V_m$$

$$V_m = \frac{E_{\max} - E_{\min}}{2}$$

Again,

$$E_{\max} = V_c + V_m$$

$$V_c = E_{\max} - V_m$$

$$= E_{\max} - \left(\frac{E_{\max} - E_{\min}}{2} \right)$$

$$= \frac{2E_{\max} - E_{\max} + E_{\min}}{2}$$

$$= \frac{E_{\max} + E_{\min}}{2}$$

$$M_a = \frac{V_m}{V_c}$$

$$\frac{E_{\max} - E_{\min}}{2}$$

$$= \frac{E_{\max} + E_{\min}}{2}$$

$$W_m = 2\pi f_m$$

$$W = \frac{2\pi}{T}, \frac{1}{T} = f = 2\pi \times \frac{1}{T} = 2\pi f_m$$

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$$= \frac{E_{\max} - E_{\min}}{E_{\max} + E_{\min}} \quad \text{or,} \quad \frac{V_{\max} - V_{\min}}{V_{\max} + V_{\min}}$$

Q1) An audio frequency signal $10 \sin 2\pi \times 500t$ is used to amplitude modulated a carrier of $50 \sin 2\pi \times 10^5 t$. Calculate

- 1) Modulation index
- 2) Side band frequency
- 3) amplitude of each side band frequency
- 4) band width requirement
- 5) total power deliver to the load of 600Ω

Ans

$$V_m = 10 \sin 2\pi \times 500t$$

$$V_c = 50 \sin 2\pi \times 10^5 t$$

$$R = 600\Omega$$

$$V_m = 10, V_c = 50$$

$$W_m = 2\pi \times 500 = 2\pi f_m$$

$$\Rightarrow 500 \text{ Hz} = f_m$$

$$W_c = 2\pi \times 10^5 = 2\pi f_m$$

$$\Rightarrow 10^5 \text{ Hz} = f_m$$

$$1) \quad M_a = \frac{V_m}{V_c} = \frac{10}{50} = \frac{1}{5} = 0.2$$

$$2) \quad f_c + f_m, f_c - f_m$$

$$\text{USB} = f_c + f_m$$

$$= 10^5 + 500 \text{ Hz}$$

$$\text{LSB} = 10^5 - 500 \text{ Hz}$$

$$3) \frac{MaV_c}{2} = \frac{0.2 \times 50}{2} \\ = 5V$$

$$\frac{-MaV_c}{2} = -5V$$

$$4) 2f_m = 2 \times 500 \\ = 1000 \text{ Hz}$$

$$\begin{aligned} 5) P_T &= P_c \left(1 + \frac{Ma^2}{2}\right) \\ &= \frac{V_c^2}{2R} \left(1 + \frac{Ma^2}{2}\right) \\ &= \frac{50^2}{2 \times 600} \left(1 + \frac{(0.2)^2}{2}\right) \\ &= \frac{2500}{1200} \left(1 + \frac{0.04}{2}\right) \\ &= \frac{25}{12} \left(\frac{2 + 0.04}{2}\right) \\ &= \frac{25 \times 2.04}{24} \\ &= 2.125 \text{ watt} \end{aligned}$$

Current relation in the amplitude modulated signal -

$$P_T = P_c \left(1 + \frac{Ma^2}{2}\right)$$

$$\frac{P_T}{P_c} = 1 + \frac{Ma^2}{2}$$

$$\Rightarrow \frac{I_t^2 R}{I_c^2 R} = 1 + \frac{Ma^2}{2}$$

$$\Rightarrow I_t^2 = I_c^2 \left(1 + \frac{Ma^2}{2} \right)$$

$$\Rightarrow I_t = I_c \sqrt{\left(1 + \frac{Ma^2}{2} \right)}$$

Efficiency of transmission - In the amplitude modulator signal have three frequency component but the message is transmitted by the side band.

Here, carrier doesn't contain any information

So efficiency of transmission is defined as the ratio of power associated with the side band frequency to the total power transmitted.

$$\eta = \frac{P_{USB} + P_{LSB}}{P_t}$$

$$\eta = \frac{P_{USB} + P_{LSB}}{P_t}$$

$$= \frac{\frac{Ma^2 V_c^2}{8R} + \frac{Ma^2 V_c^2}{8R}}{P_c \left(1 + \frac{Ma^2}{2} \right)}$$

$$= \frac{\frac{Ma^2 V_c^2 + Ma^2 V_c^2}{8R}}{P_c \left(1 + \frac{Ma^2}{2} \right)}$$

$$= \frac{\frac{2Ma^2 V_c^2}{4 \cdot 8R}}{P_c \left(1 + \frac{Ma^2}{2} \right)}$$

$$= \frac{2Ma^2 V_c^2}{4 \cdot 8R} \cdot \frac{1}{P_c \left(1 + \frac{Ma^2}{2} \right)}$$

$$= \frac{\frac{Ma^2}{2}}{1 + \frac{Ma^2}{2}}$$

$$= \frac{\frac{Ma^2}{2}}{\frac{2 + Ma^2}{2}}$$

$$= \frac{Ma^2}{2 + Ma^2}$$

$$n = \frac{Ma^2}{2 + Ma^2}$$

$$n\% = \frac{Ma^2}{2 + Ma^2} \times 100$$

$$\text{If } Ma = 1$$

$$= \frac{(1)^2}{2 + (1)^2} \times 100$$

$$= \frac{1}{2 + 1} \times 100$$

$$= \frac{1}{3} \times 100$$

$$= 33.3\%$$

From the above calculation it is concluded that when $Ma = 1$, then 33.3% of total power is carried by the side band and the rest of the power that's nearly 67% of the power is carried by the carrier which is not used. Because no useful information is carried out by the unmodulated carrier. There is the major reason of limitation of AM system (DSB-FC) for which another modulation technique DSB-SC will come into the picture.

Generation of DSB-SC signal -

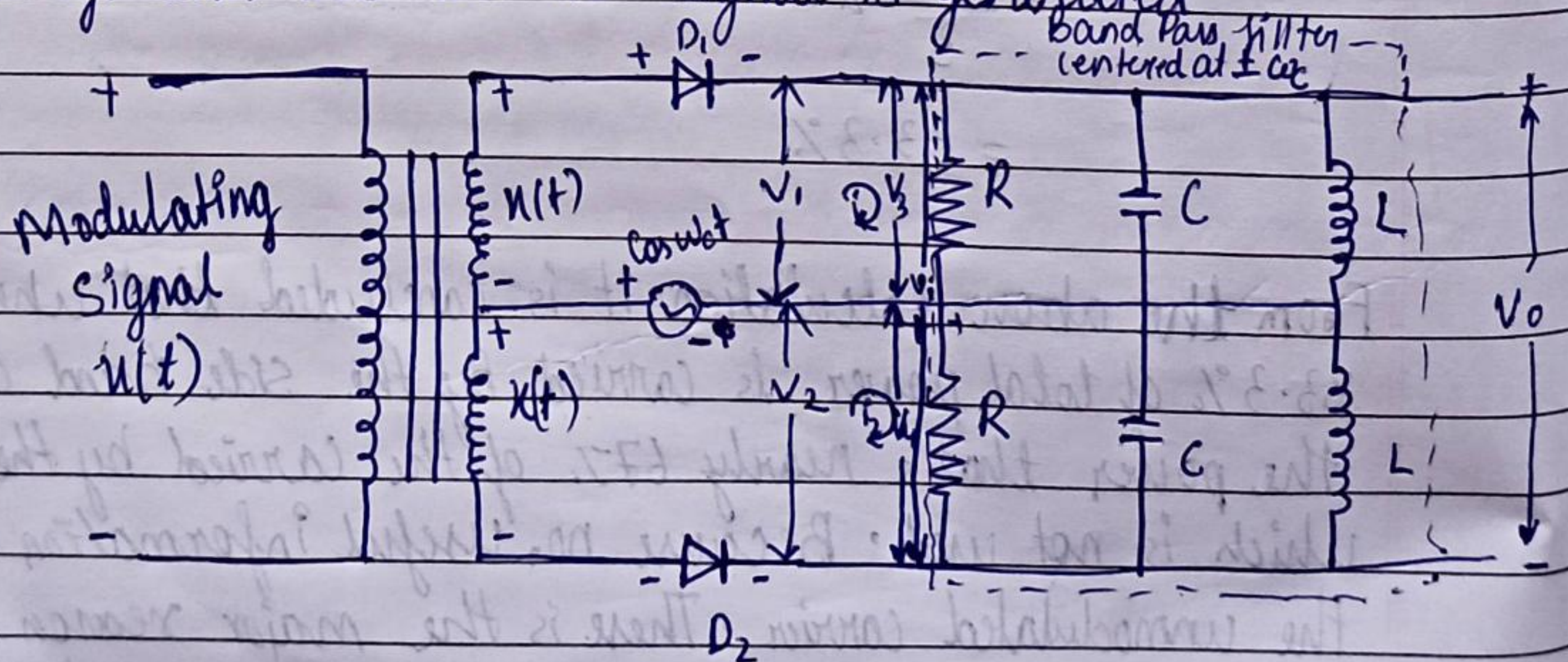
$$S(t) = u(t) \cdot \cos \omega_c t$$

Where, $u(t)$ = Modulating signal
 $\cos \omega_c t$ = Carrier signal

From the above expression we see that a DSB-SC signal is the product of modulating signal and the carrier signal. But a single device cannot generate DSB-SC signal. The circuit which generate DSB-SC signal is called a product modulator. Here we will discuss two types of product modulator. ① Balanced Modulator

② Ring Modulator

- Balanced Modulator** - We know that a non-linear device may be used produce amplitude modulated signal that's one carrier and two non-linear devices are used in a balanced mode. So, that carrier can be suppressed only by side band are left and DSB-SC AC signal is generated.



(Balanced Modulator using diodes)

∴ Rectifier - AC to DC

Filter - who ~~filter~~ gives the pure signal.

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Balanced modulation is a type of product modulator which generate DSB-SC signal using two diodes. where the modulating signal $m(t)$ is applied to the diode through the circuit center tapped transformer with the carrier signal. As the non-linear relationship between voltage and current is given by -

$$i = av + bv^2$$

In the above expression,

V is the input voltage to the diode & i is the current flowing through the diode.

Here V_1 and V_2 are two input voltage, ^{across two diodes} expressed as -

$$V_1 = \cos \omega_c t + m(t)$$

$$V_2 = \cos \omega_c t - m(t)$$

For diode D_1 the VI relationship is given by

$$i_1 = aV_1 + bV_1^2 \quad \text{--- (1)}$$

$$= a[\cos \omega_c t + m(t)] + b[\cos \omega_c t + m(t)]^2$$

$$= a\cos \omega_c t + am(t) + b[\cos^2 \omega_c t + 2\cos \omega_c t \cdot m(t) + m(t)^2]$$

$$= a\cos \omega_c t + am(t) + b\cos^2 \omega_c t + 2b\cos \omega_c t \cdot m(t) + bm(t)^2$$

→ (3)

Similarly for diode D_2 the non-linear VI relationship is

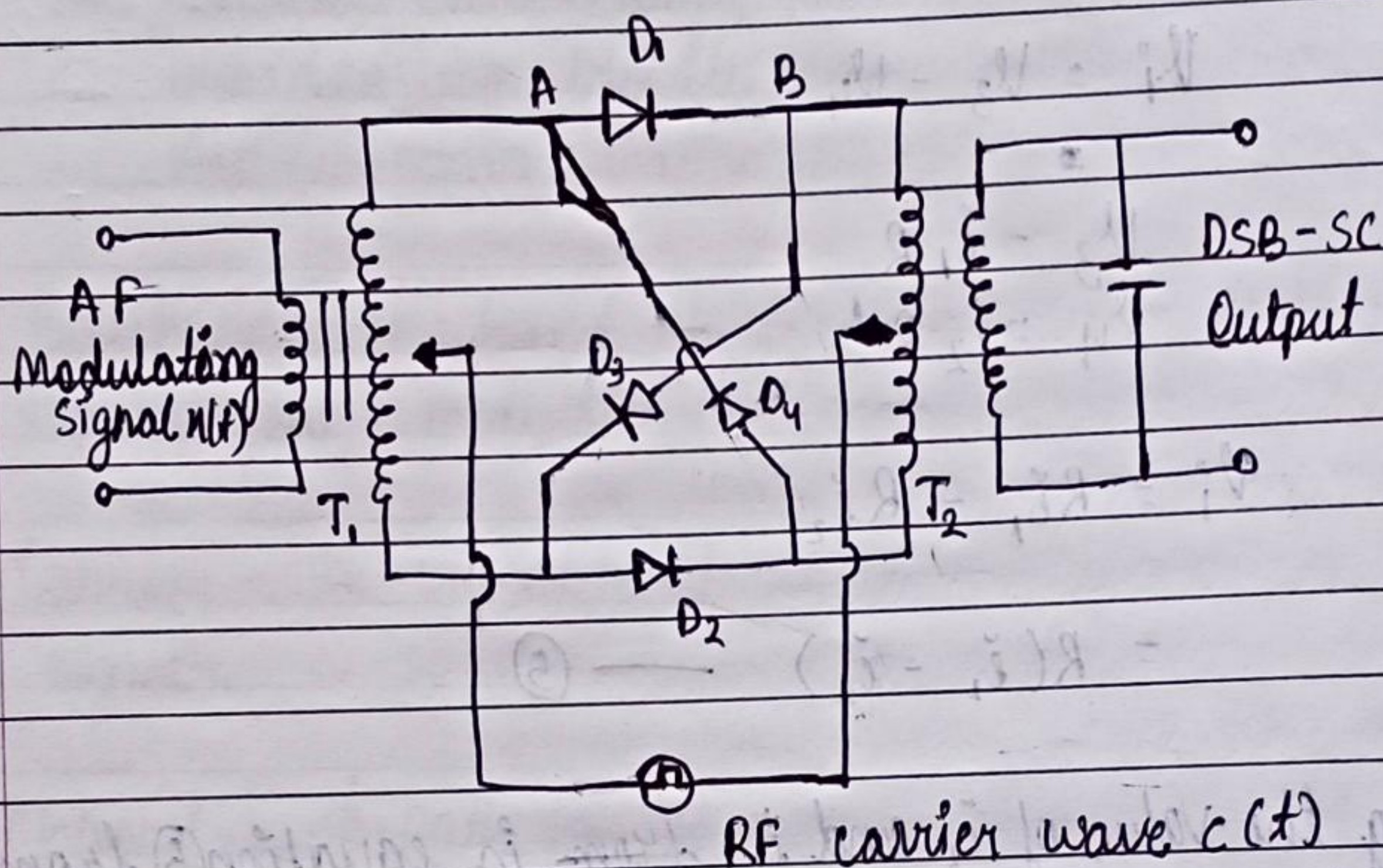
$$i_2 = aV_2 + bV_2^2 \quad \text{--- (2)}$$

$$= a[\cos \omega_c t - m(t)] + b[\cos \omega_c t - m(t)]^2$$

$$= a\cos \omega_c t - am(t) + b[\cos^2 \omega_c t + m(t)^2 - 2\cos \omega_c t \cdot m(t)]$$

$$= a\cos \omega_c t - am(t) + b\cos^2 \omega_c t + bm(t)^2 - 2b\cos \omega_c t \cdot m(t) \quad \text{--- (4)}$$

Ring Modulator -



(A diode Ring modulator)

It consists of 4 diodes, an audio frequency transformer (T_1) and RF transformer (T_2). The carrier signal is assumed to be a square wave with frequency f_c and it is connected to a center tap transformer. The DSB-SC output is obtained at the secondary of the RF transformer T_2 .

Working operation - The operation is explained with the assumption that the diodes act as perfect switches and they are switched ON and OFF by the RF carrier signal. This is because the amplitude and frequency of the carrier is higher than that of the modulating signal.

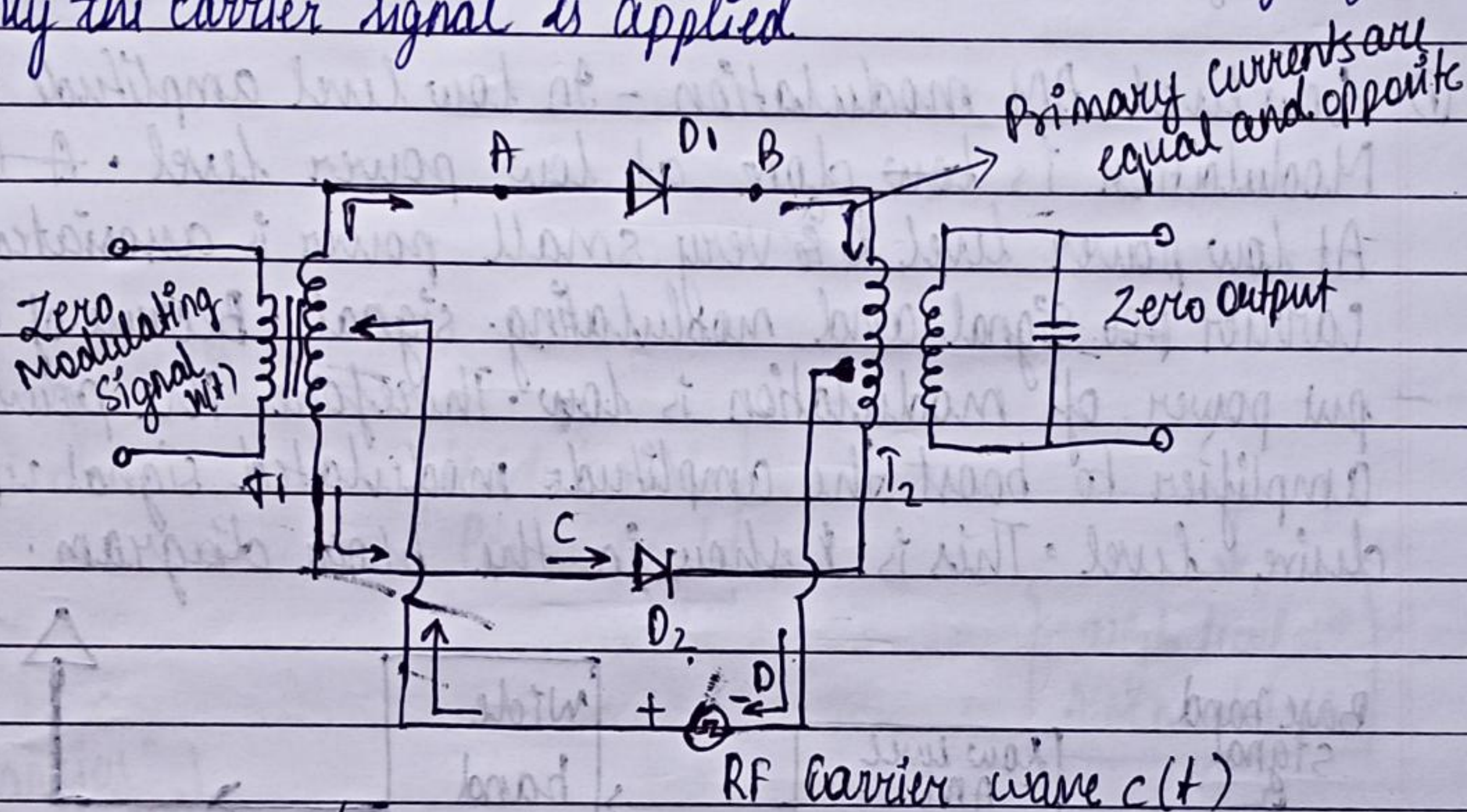
Mode-1 & Carrier Suppression -

Let us assume that the modulating signal is ~~applied~~ ^{applied}

and only the carrier signal is applied. Hence, $x(t) = 0$.

OPERATION IN THE POSITIVE HALF CYCLE OF CARRIER -

In this mode let us assume that the modulating signal is 0 and only the carrier signal is applied.

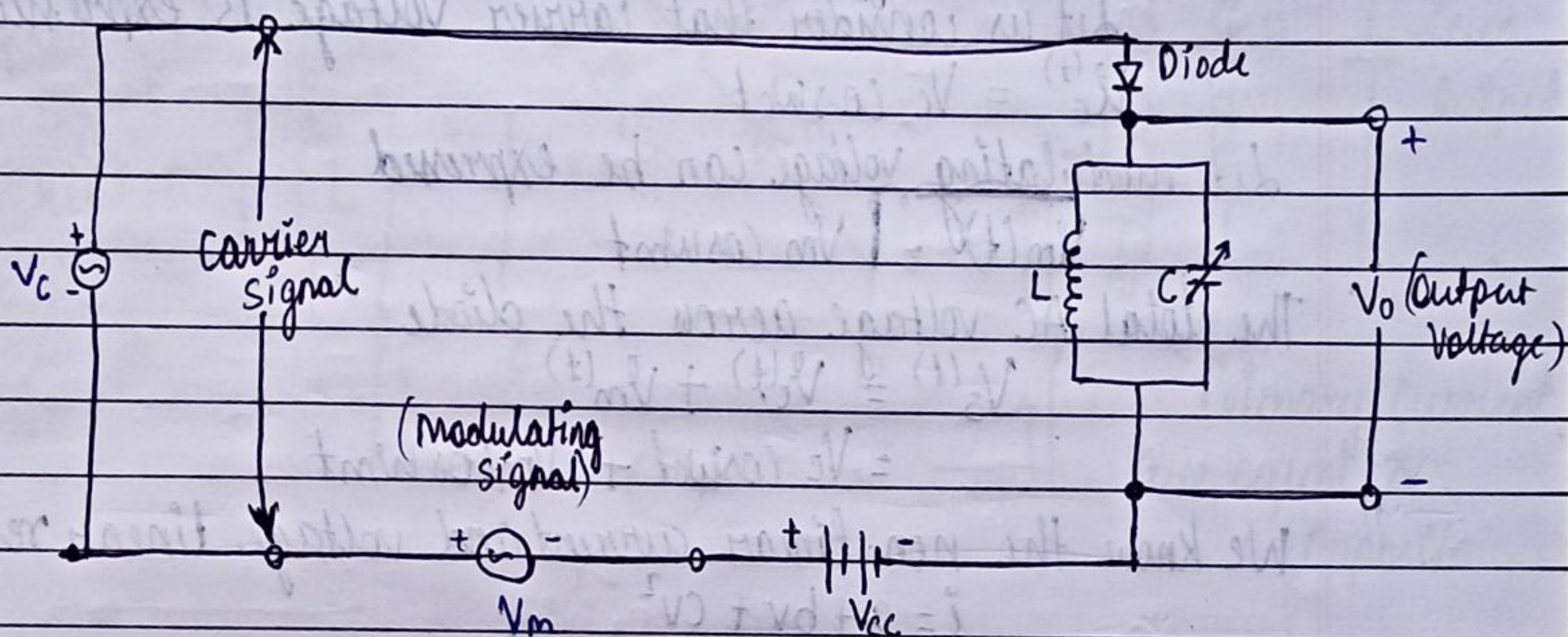


(A diode Ring modulator)

In this mode the diodes D_1 and D_2 are forward bias, Diode D_3 and D_4 are reversed bias. Let us observe the direction of currents flowing through the primary winding of output transformer T_2 , & they are equal and opposite to each other. Therefore the magnetic field produced by these currents are equal and opposite and cancel each other. Hence the induced voltage in the secondary winding is zero. Thus the carrier is suppressed in the positive half cycle.

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Square law diode modulation -



Square-law diode modulation

Defination- Square law diode modulation circuit use non-linear current voltage characteristics of diode.

→ Circuit diagram (description) -

Figure shows the circuit diagram of square law diode modulation.

Working -

Here - Carrier and modulating signals are applied across the diode.

- A DC Battery V_{cc} is connected across the diode to get fir operating point on the VI characteristic of diode.
- When carrier and ~~for~~ modulating frequency are applied at the input of diode different frequency ~~terms~~ ^{terms} appear at the output of the diode.
- These different frequency ~~terms~~ ^{terms} are applied across a tuned circuit which is tuned to the carrier frequency and just pass two

side band and reject other frequency.

Mathematical analysis -

Let us consider that carrier voltage is expressed as

$$V_c(t) = V_c \cos \omega_c t$$

Let modulating voltage can be expressed

$$V_m(t) = V_m \cos \omega_m t$$

The total AC voltage across the diode

$$V_s(t) = V_c(t) + V_m(t)$$

$$= V_c \cos \omega_c t + V_m \cos \omega_m t$$

We know the non-linear current and voltage linear relationship -

$$i = a + bv + cv^2$$

$$= a + bV_s(t) + cV_s(t)^2$$

From the above equation -

$$i = a + b(V_c \cos \omega_c t + V_m \cos \omega_m t) + c(V_c \cos \omega_c t + V_m \cos \omega_m t)^2$$

$$= a + bV_c \cos \omega_c t + bV_m \cos \omega_m t + cV_c^2 \cos^2 \omega_c t + cV_m^2 \cos^2 \omega_m t + 2cV_c V_m \cos \omega_c t \cos \omega_m t$$

$$= a + bV_c \cos \omega_c t + bV_m \cos \omega_m t + cV_c^2 \cos^2 \omega_c t + cV_m^2 \cos^2 \omega_m t + 2cV_c V_m \cos \omega_c t \cos \omega_m t$$

$$= a + bV_c \cos \omega_c t + bV_m \cos \omega_m t + \frac{cV_c^2}{2} (1 + \cos 2\omega_c t) + \frac{cV_m^2}{2} (1 + \cos 2\omega_m t) + cV_c V_m \cos(\omega_c + \omega_m)t + cV_c V_m \cos(\omega_c - \omega_m)t$$

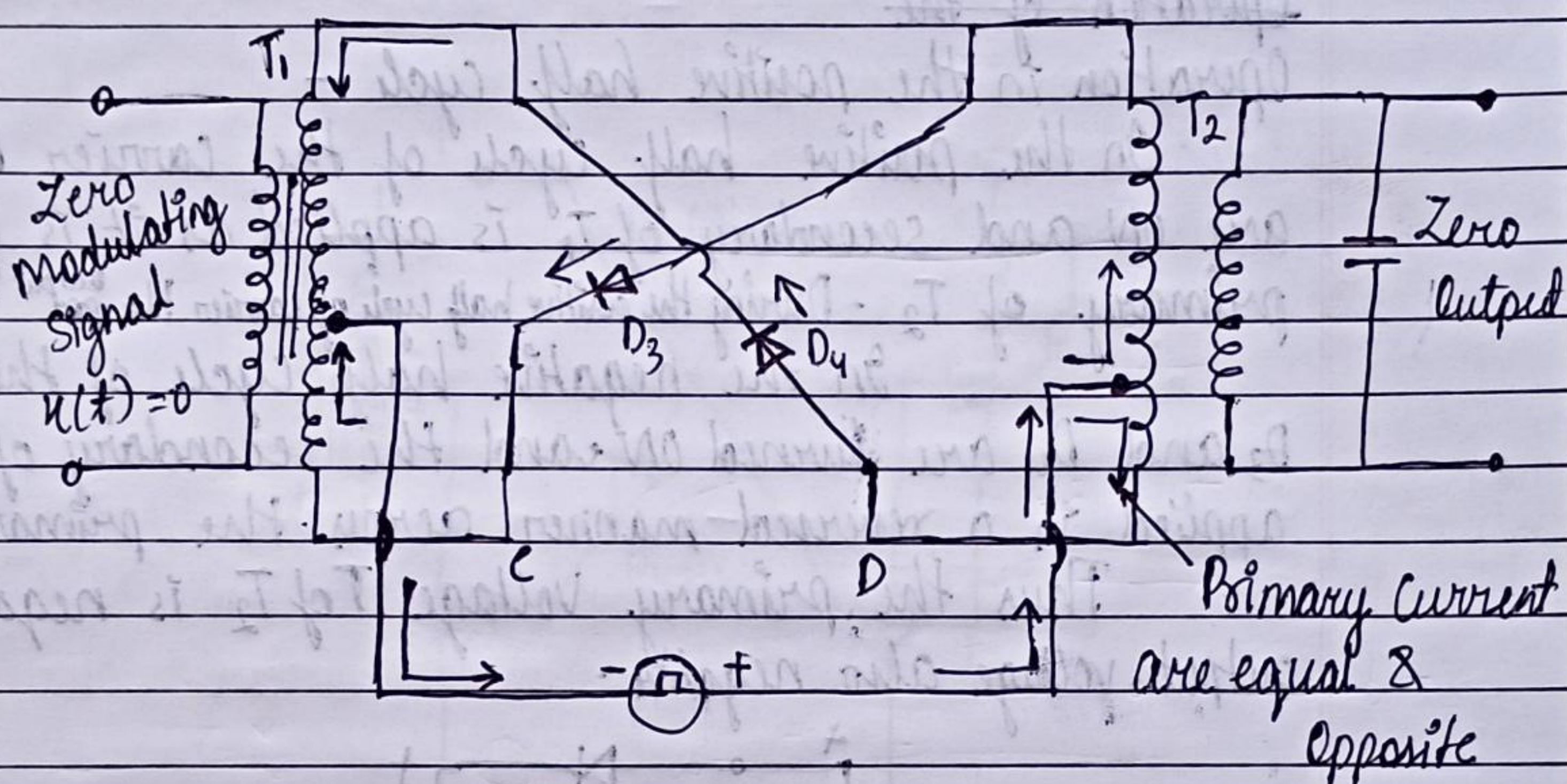
$$= a + bV_c \cos \omega_c t + bV_m \cos \omega_m t + \frac{cV_c^2}{2} (1 + \cos 2\omega_c t) + \frac{cV_m^2}{2} (1 + \cos 2\omega_m t) + cV_c V_m \cos(\omega_c + \omega_m)t + cV_c V_m \cos(\omega_c - \omega_m)t$$

$$= a + \frac{cV_c^2}{2} + \frac{cV_m^2}{2} + bV_c \cos \omega_c t + bV_m \cos \omega_m t + \frac{cV_c^2}{2} \cos 2\omega_c t + \frac{cV_m^2}{2} \cos 2\omega_m t + cV_c V_m \cos(\omega_c + \omega_m)t + cV_c V_m \cos(\omega_c - \omega_m)t$$

$$i_o = bV_c \cos \omega_c t + cV_c V_m \cos(\omega_c + \omega_m)t + cV_c V_m \cos(\omega_c - \omega_m)t$$

Next step

Operation of in negative half cycle of the carrier -



Let us assume that the modulating signal is zero. In the negative half cycle of the carrier the diode D_3 and D_4 are forward biased and the diodes D_1 and D_2 are reversed biased. The currents flowing in the upper and lower half of the primary winding of T_2 are again equal and in opposite direction. There is going to cancel the magnetic fields and the output voltage is zero. Thus the output carrier is suppressed in the negative half cycle. The perfect cancellation of the carrier will take place if and only if the characteristics of the diodes are perfectly matched and the center tap is placed exactly at the centre of the primary of transformer of T_2 .

Mode - 2

Operation of in presence of modulating signals -

When RF carrier and modulating signals both are applied.

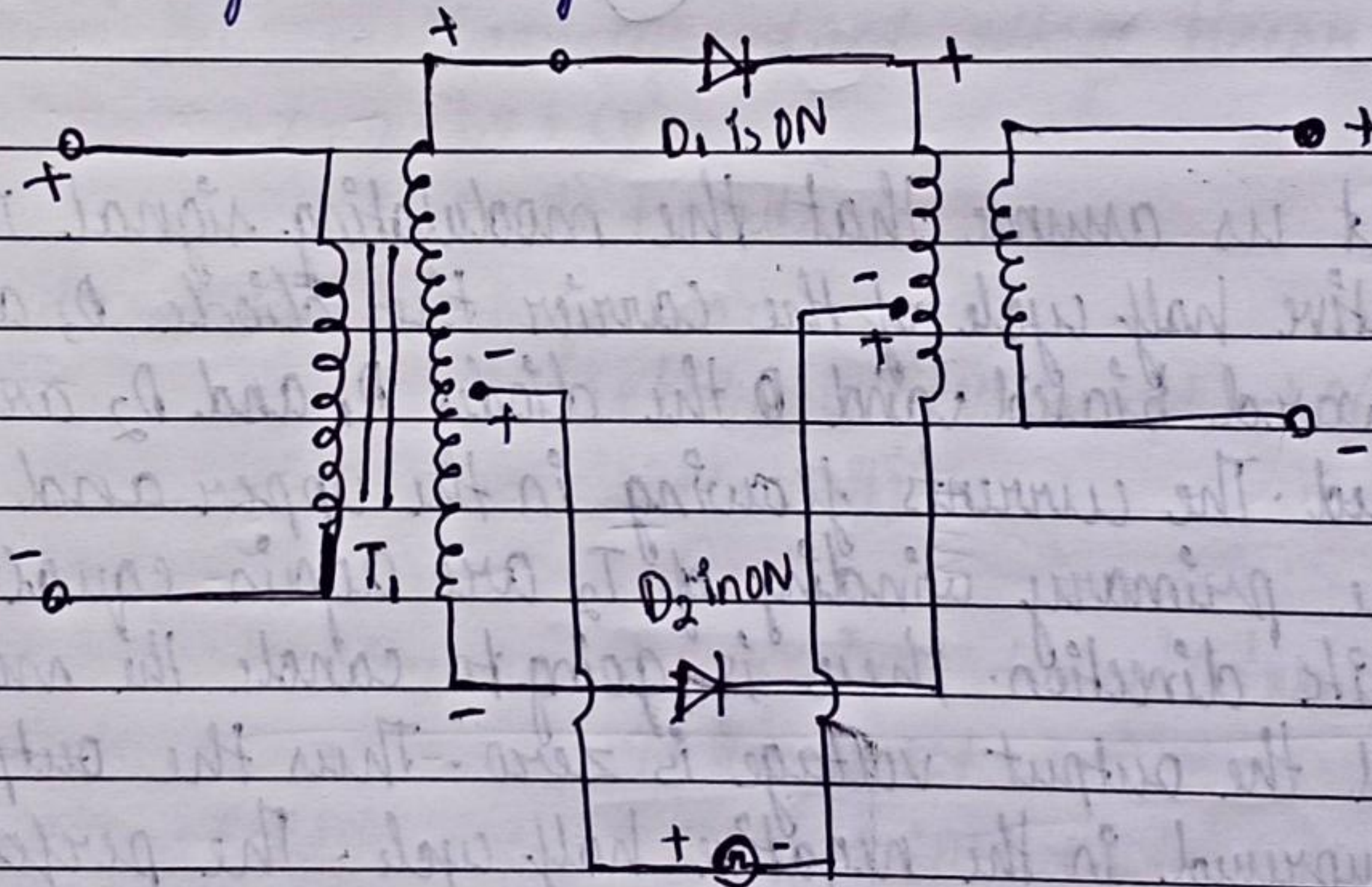
Operation of the

Operation in the positive half cycle -

In the positive half cycle of the carrier D_1 and D_2 are ON and secondary of T_1 is applied as it is across the primary of T_2 . During the positive half cycle of carrier the ^{output of T_2 is} ~~pos~~ positive.

In the negative half cycle of the carrier D_3 and D_4 are turned ON and the secondary of T_1 is applied in a reversed manner across the primary of T_2 .

Thus the primary voltage of T_2 is negative and output voltage also negative.



Equivalent circuit in the positive half cycle of modulating signal with carrier wave.

Operation in the negative half cycle of modulating signal - when modulating signal reverses the polarities the operation of the circuit is same as that in positive half cycle. Now, the only difference is that the diode pair D_3 , D_4 will produce a positive output voltage where as D_1 and D_2 will produce a negative output voltage.

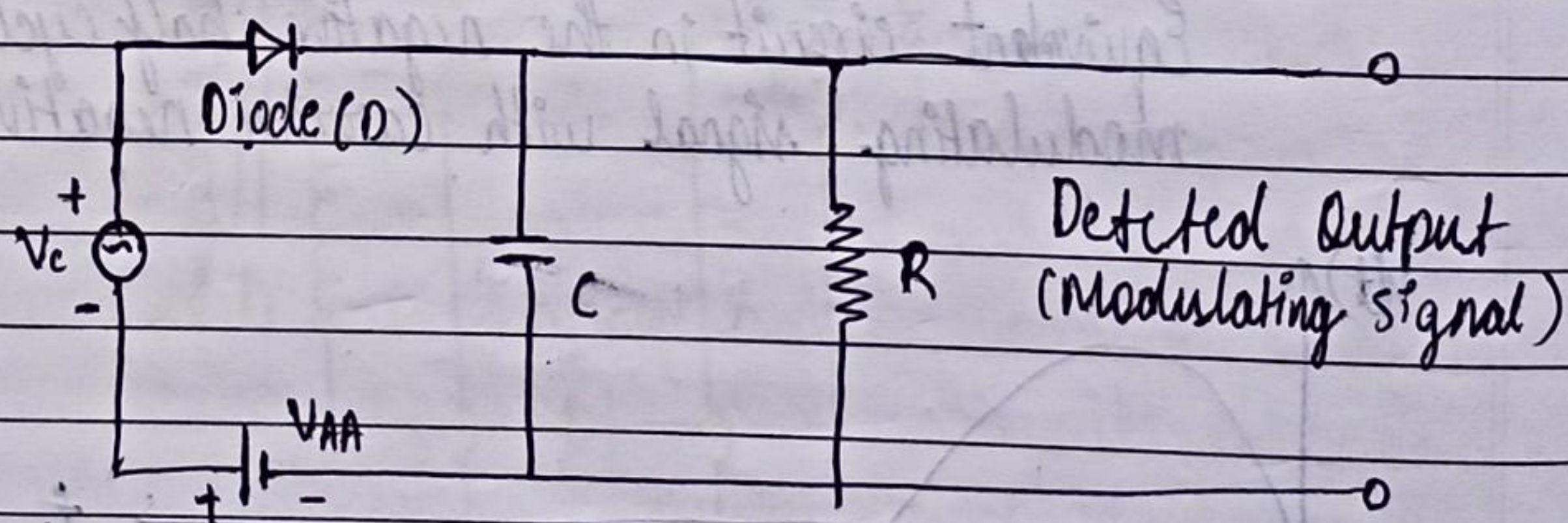
Demodulation of AM wave - The process of extracting modulating signal from the modulated signal is called demodulation or ~~the~~ detection.

There are two types of following ways -

- 1) Square law detector
- 2) Envelope law detector

Square law detector - The square law detector circuit is used for detecting modulator signal of small amplitude so that operating region restricted to the non-linear VI characteristic.

Circuit diagram -



Basic circuit of square law diode detector.

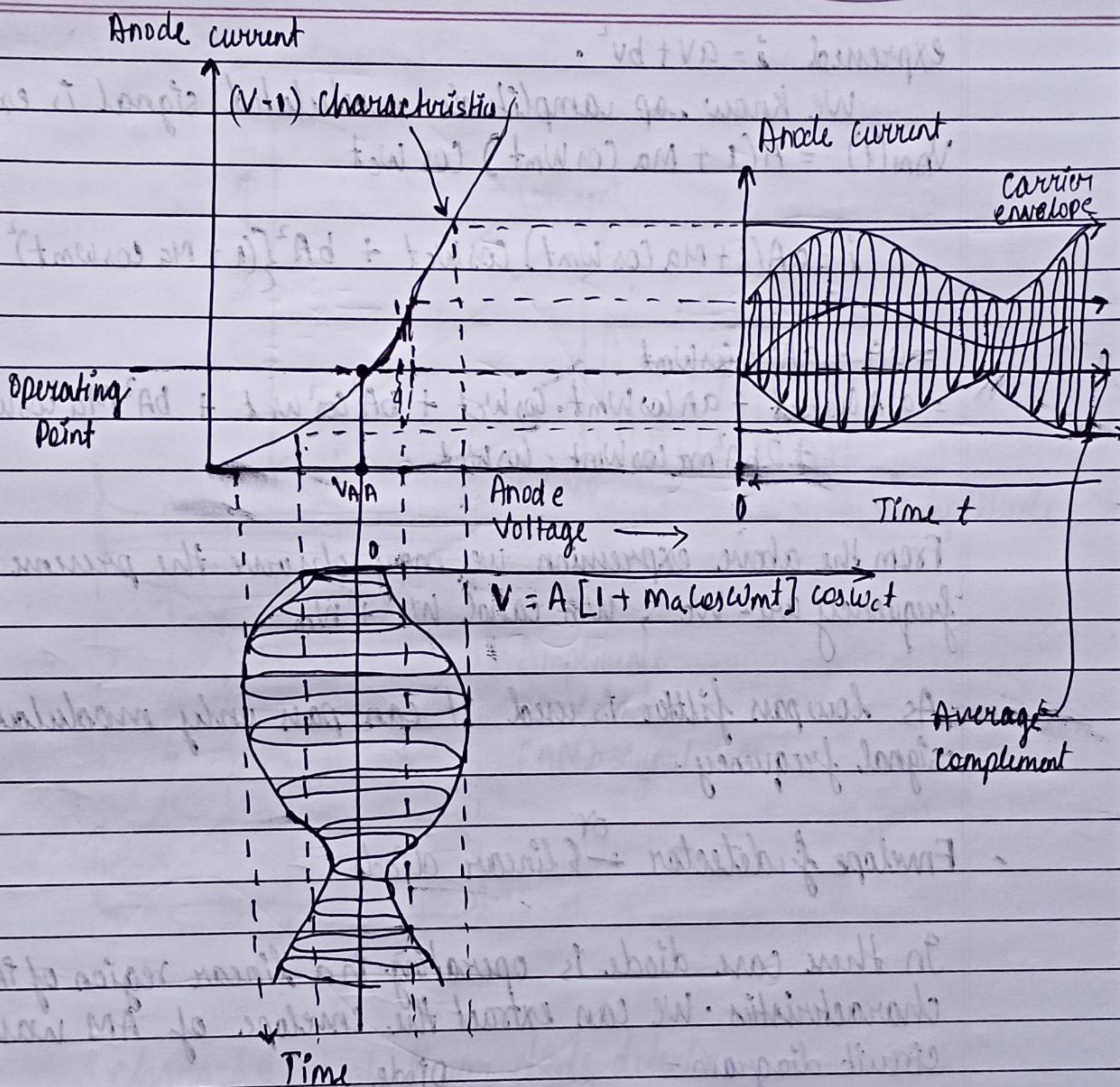


Figure shown above is the circuit diagram and VI characteristics of square law detector. In square law modulator the filter used is band pass filter where as in a square law a low pass filter is used. In these circuit, the DC supply voltage V_{AA} is used to get the fixed operating point in the non-linear portion of the diode VI characteristics. In these case the due to non-linear region the lower half portion of the modulated wave form is compressed.

The distorted output diode current is

Angle modulation system - Angle modulation may be defined as the process in which the total phase angle of a carrier wave is varied in accordance with the instantaneous value of the modulating signal while keeping the amplitude of the carrier constant.

Mathematical Representation $\rightarrow$

Let us consider that an unmodulated carrier signal is expressed as

$$c(t) = A \cos(\omega_c t + \theta_0) \quad \text{--- (1)}$$

where A = Amplitude of the carrier

ω_c = Carrier frequency

θ_0 = Some phase angle

Substituting $\omega_c t + \theta_0 = \phi$, we get

$$c(t) = A \cos \phi \quad \text{--- (2)}$$

where $\phi = (\omega_c t + \theta_0)$ is the total phase angle of the carrier signal.

We may consider equation (2) as the real part of rotating phasor $Ae^{j\phi}$.

Let us denote this rotating phasor by C . So that

$$C = Ae^{j\phi} \quad \text{--- (3)}$$

$$c(t) = \operatorname{Re}(Ae^{j\phi})$$

$$c(t) = A \cdot \operatorname{Re}(e^{j\phi}) = A \cos \phi \quad \text{--- (4)}$$

This phasor C rotates at a constant angular velocity ω_c .

θ_0 is the phase angle of the unmodulated carrier at $t = 0$. From

From equation C the constant velocity ω_c of the phase ϕ is related to its total phase angle ϕ as

$$\phi = \omega_c t + \theta_0$$

Differentiating both sides of this equation with respect to t we have,

$$\omega_c = \frac{d\phi}{dt} \quad \text{--- (6)}$$

The derivative

For unmodulated carrier derivative $\frac{d\phi}{dt}$ is constant.

However this derivative $\frac{d\phi}{dt}$ may not constant with time;

These may vary by $\frac{d\phi}{dt}$ with time. Therefore the angular velocity of the phase ϕ could also vary with time.

Hence this time dependent angular velocity or angular frequency is known as instantaneous angular velocity or instantaneous angular frequency. This instantaneous angular frequency is denoted by ω_i . So $\frac{d\phi}{dt} = \omega_i$ --- (7)

where angular frequency ω_i is time dependent

From equation (4,7), we get

$$\phi = \int \omega_i dt$$

Again writing equation (4,1) of unmodulated carrier as

$$c(t) = A \cos(\omega_c t + \theta_0)$$

$$\text{or, } c(t) = A \cos \phi$$

where ϕ is the total phase angle of the unmodulated carrier expressed as

$$\phi = \omega_c t + \theta_0$$

Now, if this angle ϕ is varied according to the instantaneous value of the message or modulation signal, the carrier signal is then said to be angle modulated.

Types of angle modulation -

There are 2 types of angle modulation -

- 1) Phase modulation
- 2) Frequency modulation

Application -

Angle modulation is been used for the following applications

- 1) Radio broadcasting
- 2) Two way mobile radio
- 3) Microwave communication
- 4) TV sound transmission
- 5) Cellular Radio
- 6) Satellite communication

Phase modulation -

Phase modulation is that type of angle modulation in which phase angle ϕ is varied linearly with a base band of modulating signal $x(t)$ about an unmodulated phase angle $(\omega_c t + \phi_0)$.

The instantaneous value of the phase angle is equal to the phase angle of the unmodulated carrier $(\omega_c t + \phi_0)$ plus a time varies component which is proportional to modulating signal $x(t)$.

Mathematical representation -

We know that unmodulated carrier signal is expressed as

$$c(t) = A \cos(\omega_c t + \phi_0)$$

$$\text{or } c(t) = A \cos \phi$$

where, $\phi = \omega_c t + \phi_0$

Neglecting ϕ_0 , we get total phase angle of unmodulated

carrier is $\phi = \omega_c t$.

Now, according to phase angle modulation, this phase angle ' ϕ ' is varied linearly with a baseband or modulating signal $x(t)$.

Let the instantaneous value of phase angle be denoted by ϕ_i . Therefore,

$$\phi_i = \omega_c t + k_p x(t)$$

where k_p is the proportionality constant & known as phase sensitivity of the modulator. This is expressed in radians/volts. Since, the expression for unmodulated carrier wave is $c(t) = A \cos \phi$.

Therefore, the expression for phase modulated wave will be $s(t) = A \cos \phi_i$.

Putting the value of ϕ_i in equation (4.10) we get $s(t) = A \cos [\omega_c t + k_p x(t)]$ which is required mathematical expression for a phase modulated wave. (4.11)

Frequency modulation -

Frequency modulation is that type of angle modulation in which the instantaneous frequency is varied linearly with a message or baseband signal $x(t)$ about an unmodulated carrier frequency ω_c .

→ The instantaneous value of the angular frequency ω_i will be equal to the carrier frequency ω_c plus a time varying component proportional to the baseband signal $x(t)$.

Mathematical representation -

We know that the instantaneous frequency is given by

$$\omega_i = \omega_c + k_f \cdot x(t) \quad \text{--- (1)}$$

where k_f is proportionally constant & is known as the frequency sensitivity of the modulator. This is expressed in Hz/volt.

Now, let the expression for unmodulated carrier signal be

$$c(t) = A \cos(\omega_c t + \theta_0) \quad \text{--- (ii)}$$

$$c(t) = A \cos \phi \quad \text{--- (iii)}$$

$$\phi = \omega_c t + \theta_0 \quad \text{--- (iv)}$$

where, ϕ is the total phase angle of the unmodulated carrier.

Let ϕ_i be the instantaneous phase angle of the modulated signal. From equation (4.15) the equation for unmodulated carrier is

$$c(t) = A \cos \phi$$

On frequency modulation amplitude A must remain constant & only angle ' ϕ ' will change.

Hence, the expression for frequency modulated wave will be

$$s(t) = A \cos \phi \quad \text{--- (v)}$$

where ϕ_i = instantaneous phase angle. frequency equation (iii), we have

$$\phi = \omega_c t + \theta_0$$

On differentiation, we get

$$\frac{d\phi}{dt} = \omega_c$$

or

$$\phi = \int \omega_c dt \quad \text{--- (vi)}$$

Base on equation (vi), we may write the expression on equation instantaneous phase angle ϕ_i as

$$\phi_i = \int \omega_i dt \quad \text{--- (vii)}$$

where ω_i = instantaneous frequency modulation wave. Putting this value of ω_i in equation (vi) we get the expression for frequency modulated wave will be.

$$s(t) = A \cos [\omega_c t + k_f \int u(t) dt] \quad \text{--- (viii)}$$

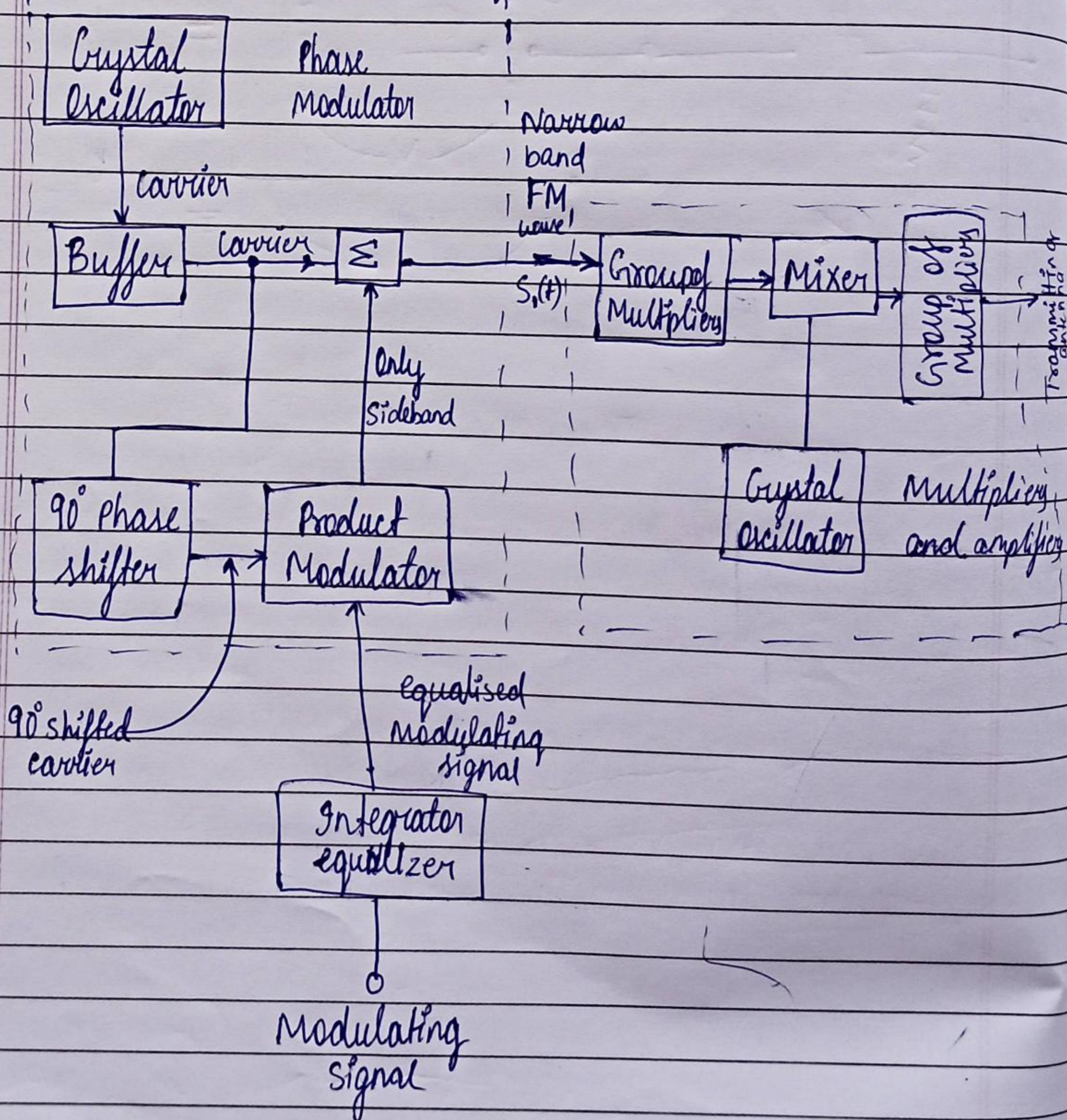
Method of FM generation -

There are two types of method -

① Direct method

② Indirect method

Indirect method (Armstrong method)



Indirect method (Armstrong method) of FM generation.

The working operation of indirect method are divided into two parts.

Part 1 -

Generate a narrow band FM wave using phase modulator.

Part 2 -

Use the frequency multipliers and mixers to obtain required values of frequency deviation carrier and modulation index.

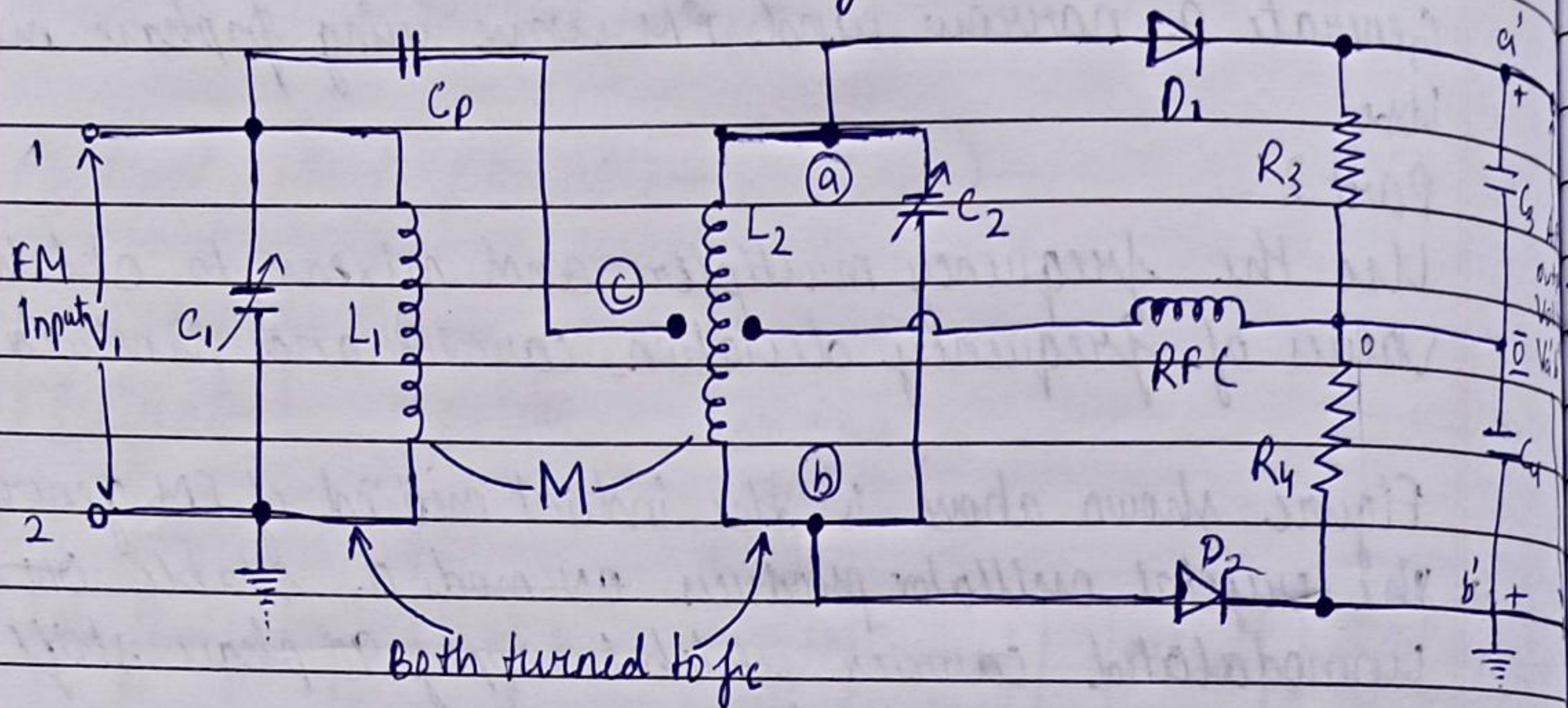
Figure shown above is the indirect method of FM generation.

- The crystal oscillator produces ~~on mod~~ a stable ~~on mod~~ unmodulated carrier which is apply 90° phase shift as well as combining network through a buffer.
- The 90° phase shifter ~~carrier~~ produces a 90° phase shifted carrier.
- It is applied to the balanced modulator. Along with modulating signal.
- Hence at the output of product modulator, we get DSB-SC signal.
- The two side band and the original carrier without any phase shift are applied to a combining network.
- The FM signal produce at the output of phase modulator, has low carrier frequency and low modulation index.
- Therefore they are increased with the help of frequency multiplier and mixer.

Demodulation of FM wave -

Demodulation of FM wave -

Phase discriminator (Foster seeley) -



Phase discriminator

Operation - Here the primary and secondary tuned circuit are tuned to the same center frequency. The voltages apply to the two diodes D_1 and D_2 are not constant.

In these case varying of the voltage depend upon frequency of the input signal.

- At input frequency (f_{in}) = f_c , the individual output voltages of the two diodes will be equal and opposites. The output voltage is zero.

$$V_o = V_{o1} - V_{o2}$$

- For $f_{in} > f_c$, the phase shift between the primary and secondary winding is such that the output of D_1 is higher than D_2 . Hence output voltage will be positive.